

Plasmon enhanced fluorescence characteristics government by selecting the right objective function

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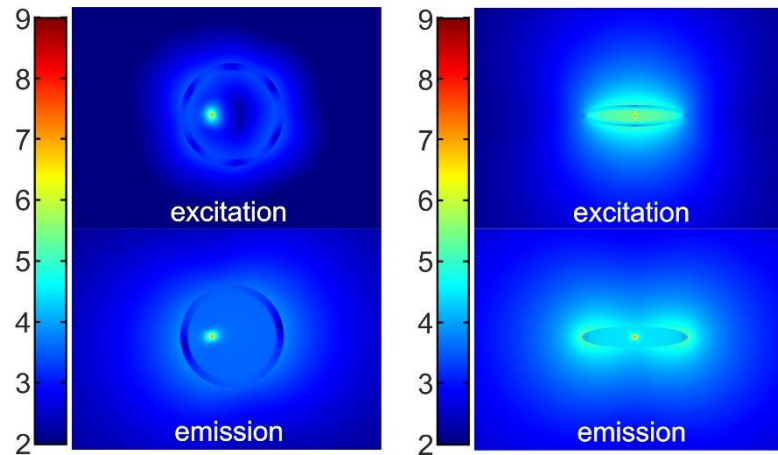
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Department of Computational Optimization

University of Szeged

COMSOL 2018



Localized surface plasmon resonance



excitation enhancement via plasmonic resonance
 emission improvement via Purcell & antenna effect

metal nanoshells as plasmonic nanoresonators
 -> smaller metal volume
 -> resonant frequency tuning via GAR
 -> ellipsoid: non-degenerated trans. and long. modes

Dicke effect

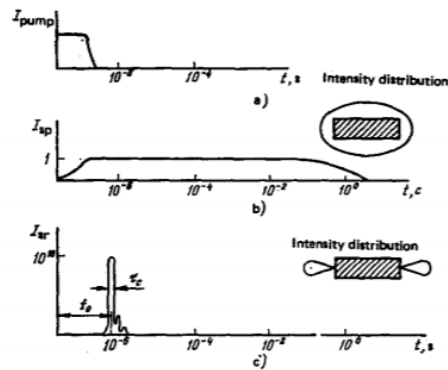
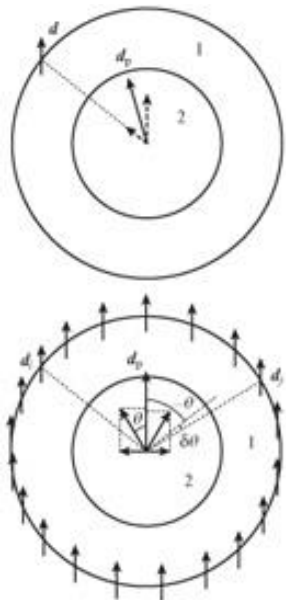


FIG. 2. Comparison of superradiance and noncoherent spontaneous emission.²⁴ The time scale is logarithmic. a) Pump pulse which creates a population inversion for the working transition, $a \rightarrow b$; b) emission intensity in the case of noncoherent spontaneous decay ($T_1 \sim 1s$): a slow exponential decay with an isotropic directional distribution of the intensity; c) the observed highly directional superradiance signal (in gaseous HF; Ref. 24). The peak intensity I_{sr} is roughly 10^{10} times I_{sp} .

emitters can radiate cooperatively

N-times shorter radiative decay:

-> N-times shorter pulse

-> emission intensity proportional to N^2

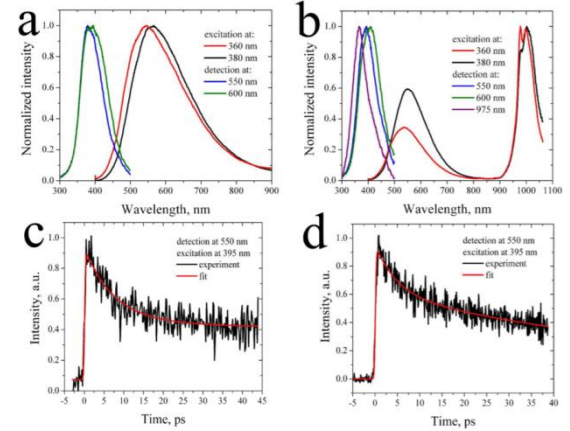
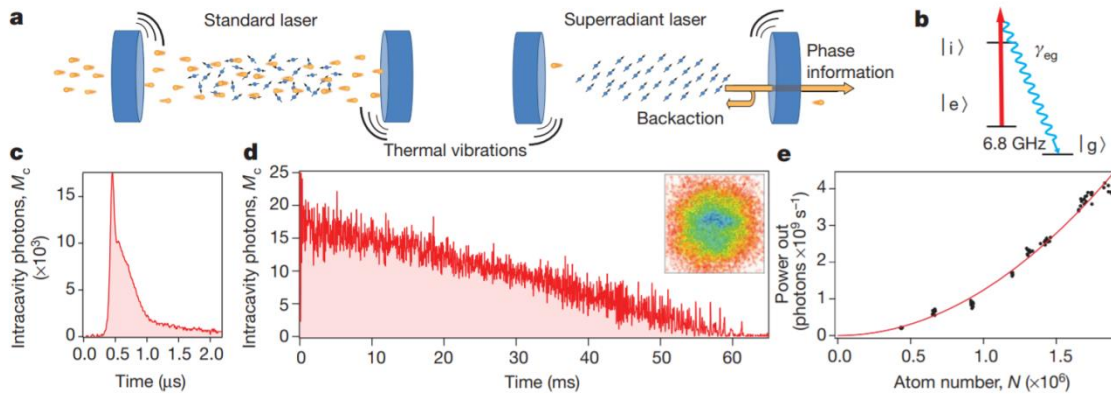
indistinguishability & ensemble volume
 smaller than the wavelength

A. Szenes *et al* Scientific Reports 7, 13845 (2017)

I. E. Protsenko and A. V. Uskov Quantum Electron. 45 561 (2015)

A. V. Andreev *et al* Sov. Phys. Usp. 23 493 (1980)

Dicke effect applications



superradiant lasers with ultra-narrow lines
(non-plasmonic)

generation of ps pulses in Ag nanoclusters

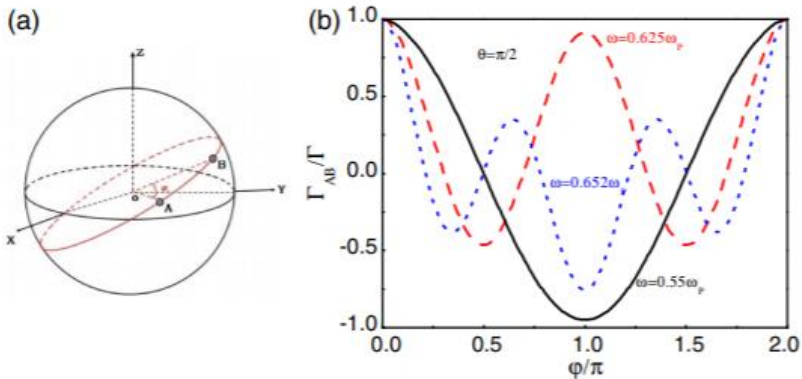
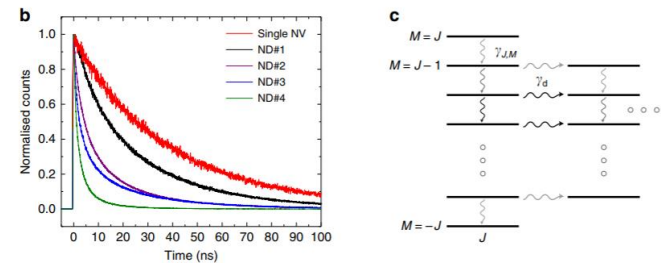
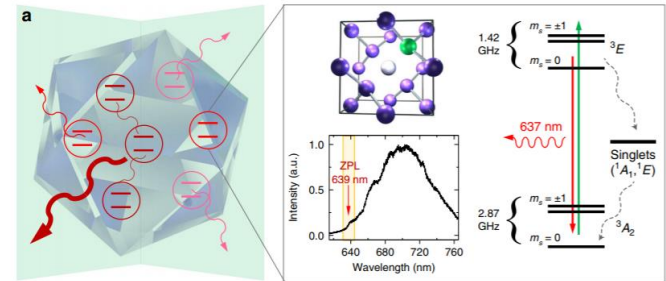


Fig. 3. (a) Positions of two emitters (A and B) near a metal nanoparticle. (b) Γ_{AB}/Γ as a function of the angle between two emitters around the sphere. The solid, dashed, and dotted lines correspond to the cases with $\omega = 0.55\omega_p$, $0.625\omega_p$, and $0.652\omega_p$, respectively. The other parameters are identical with those in Fig. 2.



multi-qubit deterministic quantum phase gate
with ordered radial arrangement

superradiance of NV centers

J. G. Bohnet Nature 484(7392), 78-81 (2012).

J. Ren *et al* J. Opt. Soc. Am. B 31(2), 229-236 (2014).

M. V. Shestakov J. Phys. Chem. C 119(34), 20051-20056 (2015).

C. Bradac *et al* Nat. Commun. 8(1), 1205 (2017).

Plasmonic Dicke effect

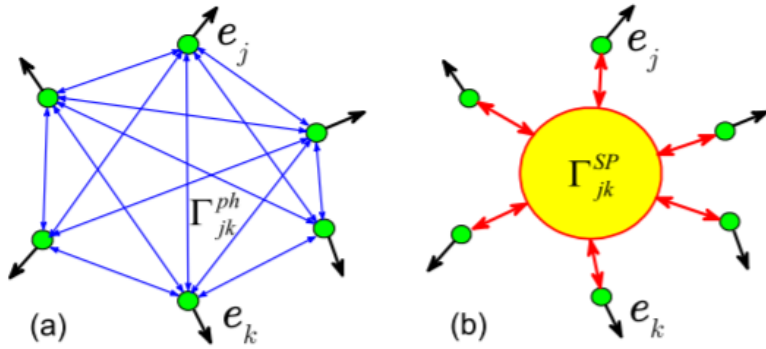


FIG. 1 (color online). (a) Radiative coupling of emitters in free space and (b) plasmonic coupling of emitters near a NP.

direct coupling through radiation
indirect coupling through plasmons

dipoles around solid NP or in concave resonator:
random phase, uniform orientation
random or CX configuration

plasmonic coupling overrides radiative coupling:
total radiative rate $\sim N/3$, total energy $3x$

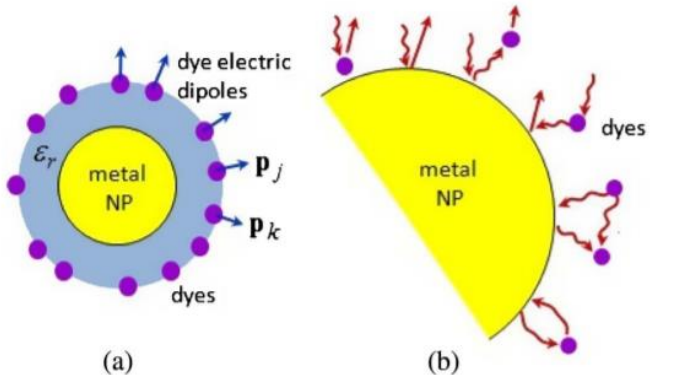


Fig. 1. (a) Aggregate made by one nanoplasmonic sphere and a layer of N dyes. (b) Some radiative and nonradiative coupling mechanisms among dyes and nanoparticle are considered.

cooperative plasmon mediated coupling
in metal NP covered by gain medium

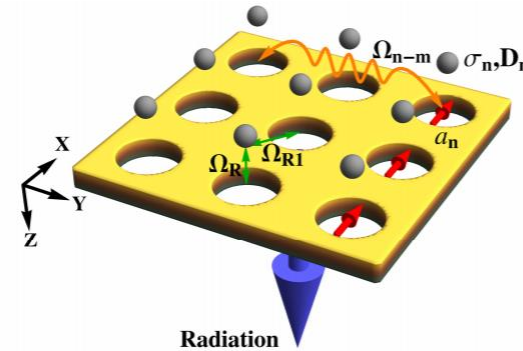


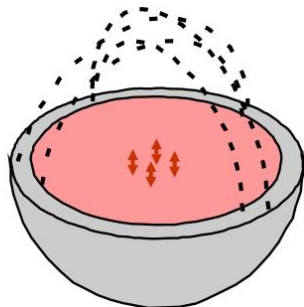
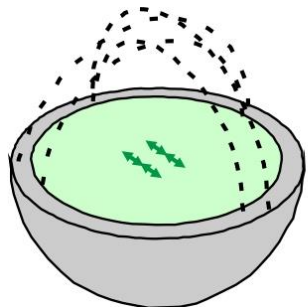
Fig. 1. Phase distribution of the plasmon oscillations in spaser arrays of (a) 5×5 and (b) 100×100 spasers. In all calculations, we use $\Delta = \lambda/20$, where λ is the free space wavelength.

CW plasmonic SR from gain molecules
coupled through plasmons on nanohole array

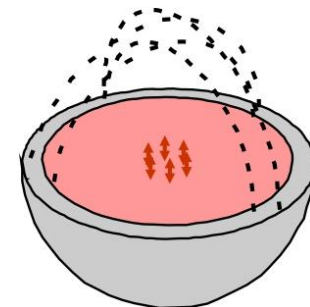
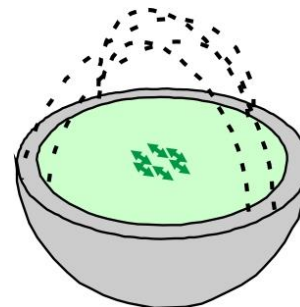
V. N. Pustovit *et al* Phys. Rev. Lett. 102(7), 077401 (2009).
J. T. Manassah Laser Phys. 22(4), 738-744 (2012).
A. V. Dorofeenko Opt. Express 21(12), 14539-14547 (2013).
V. N. Pustovit *et al* J. Opt. Soc. Am. B 32(2), 188-193 (2015).

Nanoresonator types and geometries

4iCS



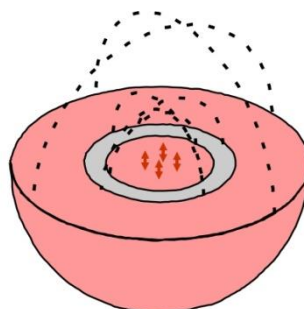
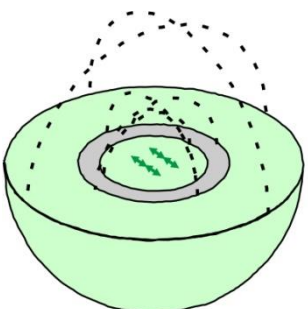
6iCS



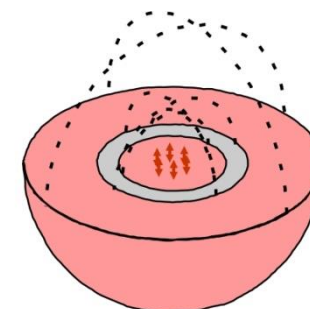
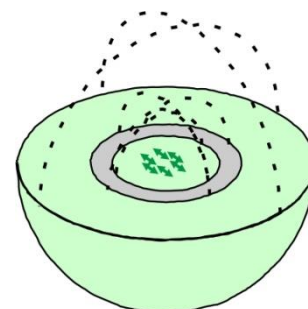
SCS-type

diamond-silver
core-shell

4iCSS



6iCSS



SCSS-type

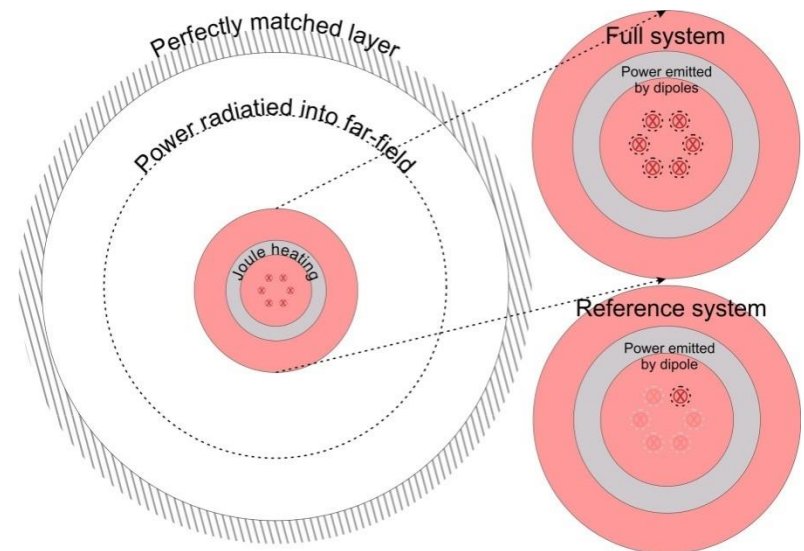
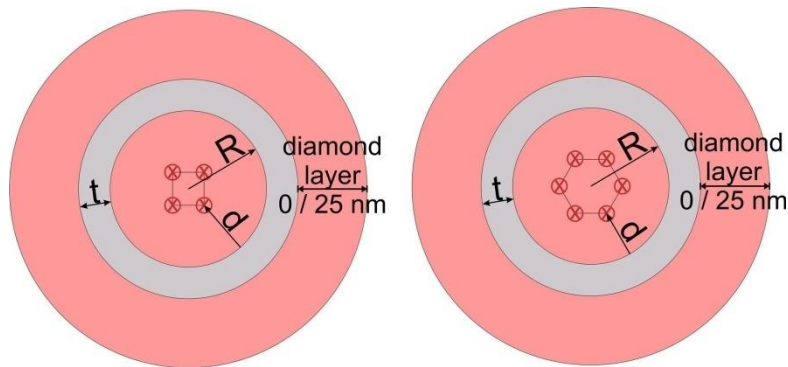
diamond-silver-diamond
core-shell-shell

Optimization-> cooperative fluorescence

- **Objective:** enhancement of **excitation** & **emission** simultaneously
- **Method:** configuration optimization (geometry and illumination condition)
- **Type** of concave core-shell nanoresonators:
 - diamond-silver core-shell (CS) and diamond-silver-diamond core-shell-shell (CSS)
- **Geometry** of concave core-shell nanoresonators:
 - spherical (SCS & SCSS) as a special kind of ellipsoidal
- **Varied parameters**
 - $2r$, t , GAR, φ , θ
- **Type of fluorescent dipoles:**
 - SiV center

coupled fluorescence qualification:

$$\delta R_{exc} = \text{Purcell}_{exc} * QE \quad \& \quad \delta R_{em} = \text{Purcell}_{em} * cQE$$



evaluation of superradiance:
comparison with the reference system

Conditional optimization

$P_x = \delta R_{exc} * \delta R_{em}$: total fluorescence rate enhancement optimization

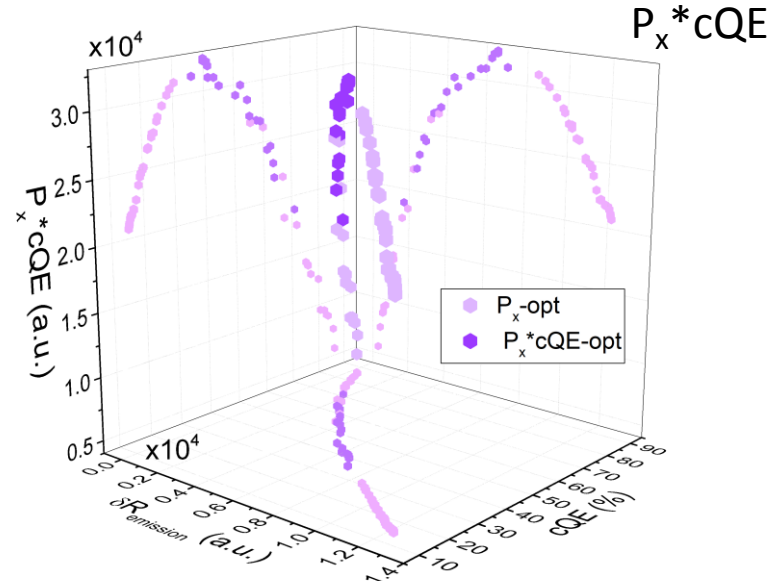
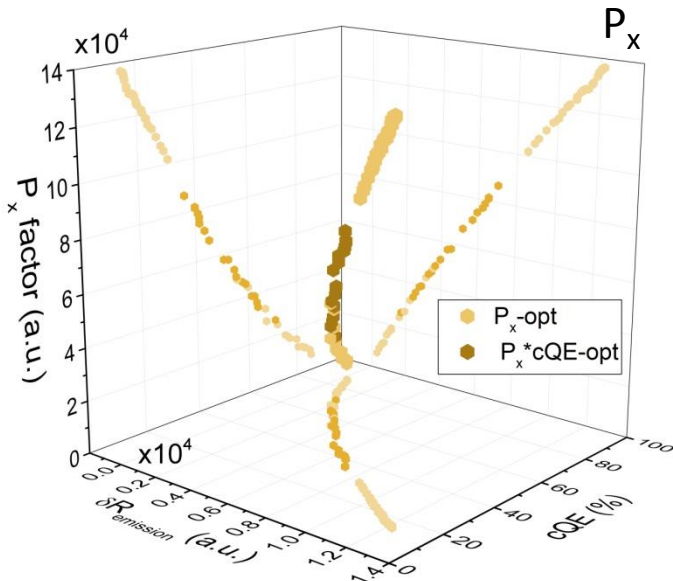
$P_x * cQE = \delta R_{exc} * \delta R_{em} * cQE$: weighted composite objective function optimization

radiative rate enhancement & corrected cQE criteria ->
excitation improvement & multiple cQE mapped

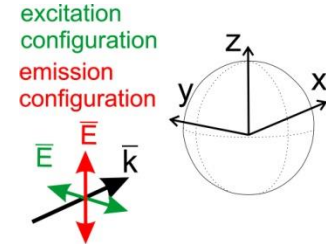
GLOBAL implemented via LiveLink for MATLAB: Sampling (Monte Carlo), Clustering (Single-link),
Local searching (UNIRANDI, Random walk, BFGS)

T. Csendes et al.: The GLOBAL Optimization Method Revisited, Optimization Letters 2 (2008) 445-454

B. Bánhelyi et al.: The GLOBAL optimization algorithm. Newly Updated with Java Implementation and Parallelization. Springer Briefs on Optimization, accepted (2018)



Optimization-> cooperative fluorescence



Extracted quantities

nanoresonator qualification: **ecs, scs** & **ecs, scs**

coupled fluorescence qualification: $\delta R_{exc} = \text{Purcell}_{exc} * QE$ & $\delta R_{em} = \text{Purcell}_{em} * cQE$

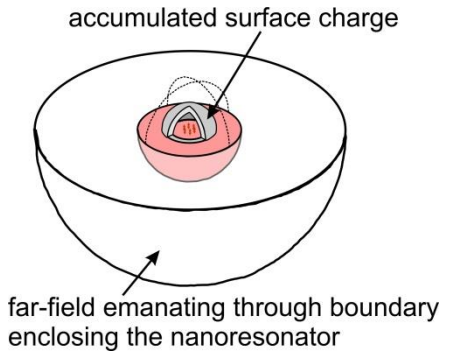
accompanying nanophotonical phenomena: **charge, far-field** (\hat{y}) & **charge, far-field** (\hat{z})

evaluation of nanoresonators: **ecs, scs** -> FWHM -> Q,

evaluation of coupled systems: Purcell, δR -> FWHM -> Q; $\Delta\lambda$ & Δf

evaluation of superradiance: comparison with the reference system

$r\delta R_{exc}$, $r\delta R_{em}$, $rcQE$, rP_x , $rP_x * cQE \Leftrightarrow N^2, \Rightarrow rX_{average}$

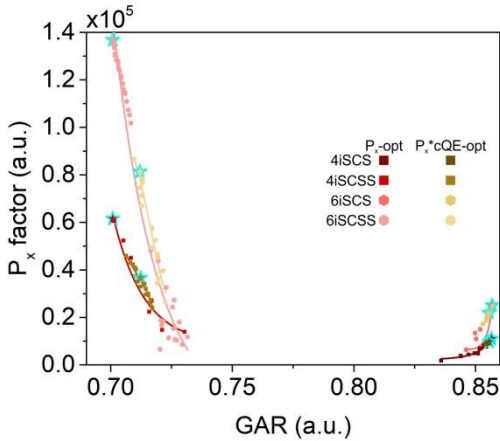
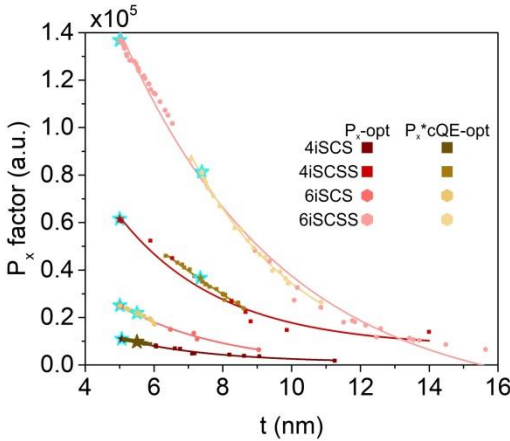
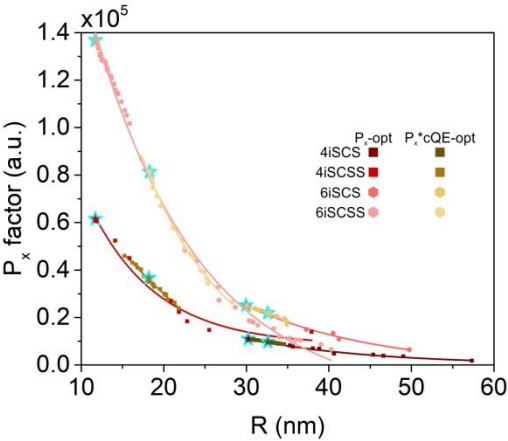


ranking of nanoresonators taking into account P_x , $P_x * cQE$, cQE , $rX_{average}$, $Q_{Purcell}$, $\Delta\lambda$

FOM evaluation:

dependency of P_x and $P_x * cQE$ on geometrical parameters, $P_x(cQE)$, $P_x * cQE(P_x)$, $P_x * cQE(cQE)$

Dependence of the P_x FOM on geometry

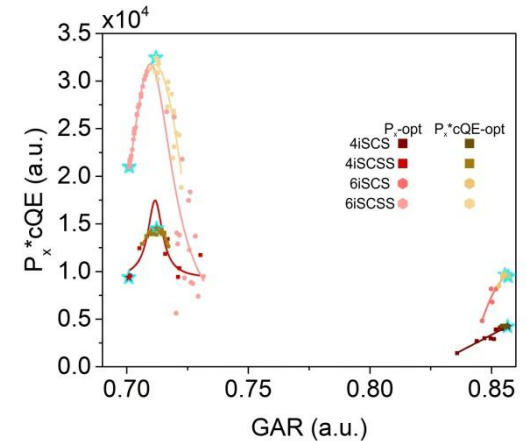
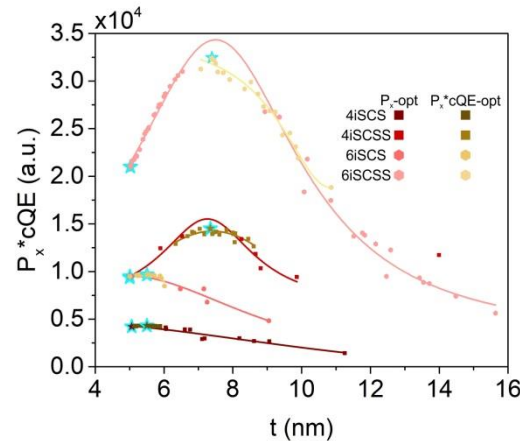
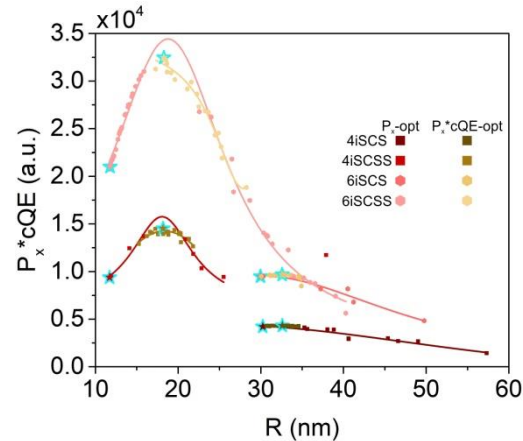


fitting for nanoresonators determined via different FOMs independently
 fitted curves overlap

P_x monotonously modifies

$P_x \Leftrightarrow P_x^*cQE$, $4 \Leftrightarrow 6$, $SCS \Leftrightarrow SCSS$
 fitted function takes on larger values

Dependence of the P_x^*cQE FOM on the geometry



fitting for nanoresonators determined via different FOMs independently

fitted curves overlap

$P_x^*cQE \Leftrightarrow P_x$

fitted functions take on larger values

- P_x^*cQE nanoresonators:

maximum as a function of all nanoresonator parameters (R , t , GAR) (e: 6iSCSS, outside)

- P_x nanoresonators:

-inside interval in 4iSCSS and 6iSCSS,

-outside interval for R , t , GAR in 6iSCS & for R dependency in 4iSCS,

no maximum for t and GAR dependency in 4iSCS

$4 \Leftrightarrow 6$

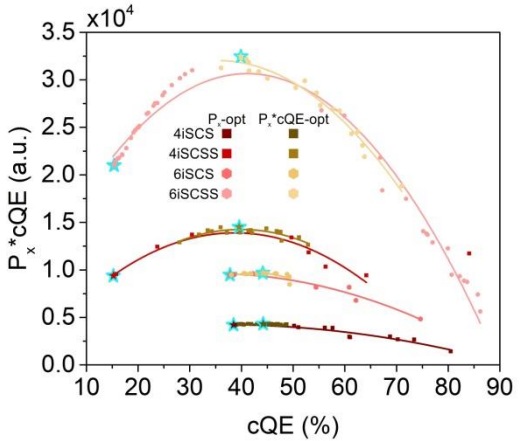
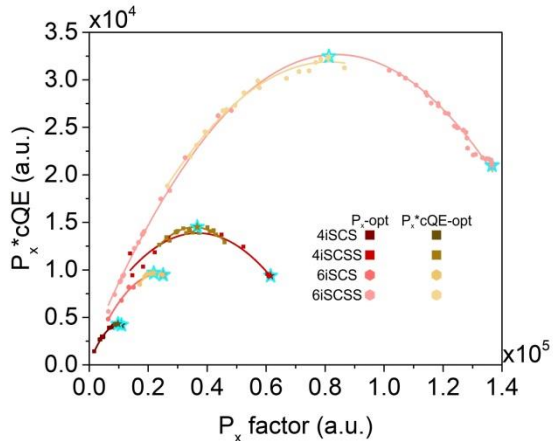
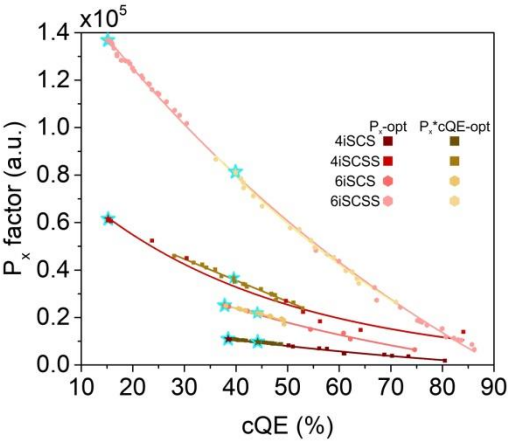
fitted functions take on larger values

SCS \Leftrightarrow SCSS

fitted functions take on larger values

parameter intervals of maxima in R / t / GAR are bounding / overlapping / different

Dependence of the FOMs on P_x & cQE/cQE

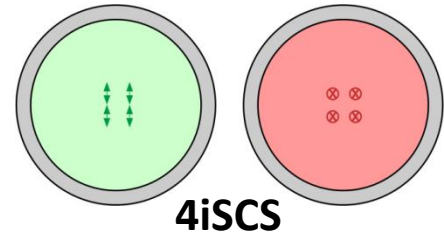


P_x
 exponential decay as a function of cQE

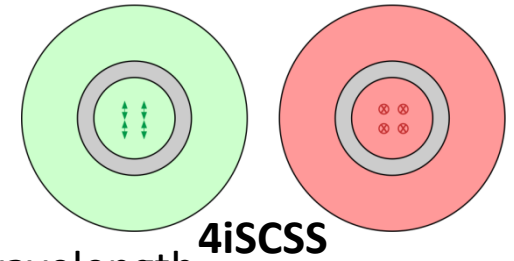
P_x *cQE

- P_x *cQE nanoresonators
 P_x *cQE exhibits a maximum as a function of P_x & cQE
 (exception 6iSCSS, outside the cQE interval)

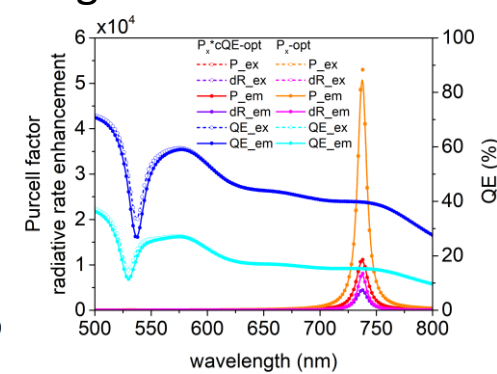
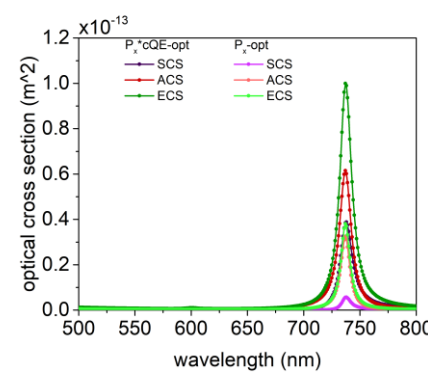
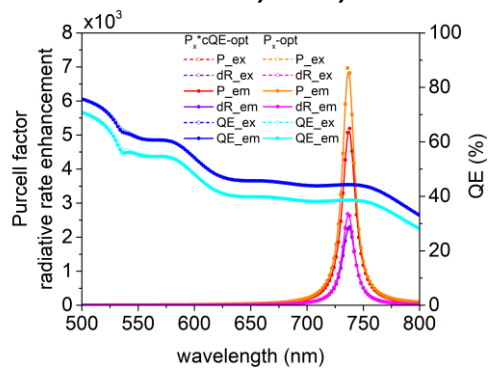
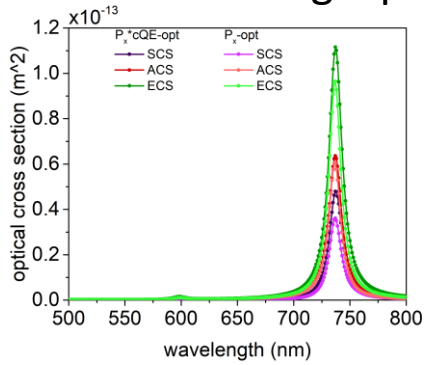
- P_x nanoresonators
 4iSCSS and 6iSCSS exhibit a maximum as a function of P_x & cQE
 4iSCS and 6iSCS as a function of cQE outside interval of representative points



$$P_x \Leftrightarrow P_x^* \text{cQE: right FOM}$$



Single peak on the ecs, scs, Purcell, δR at the emission wavelength



$(I_{\min}) I_{\max}$ on QE at (exc) emission

(g_{\min}) plateau/decrease on QE at (exc) emission
for $P_x / P_x^* \text{cQE}$

$$P_x \Leftrightarrow P_x^* \text{cQE - geometry}$$

larger core, thicker shell, similar GAR,
larger dipole distance

$$P_x \Leftrightarrow P_x^* \text{cQE - optical response}$$

-QE larger

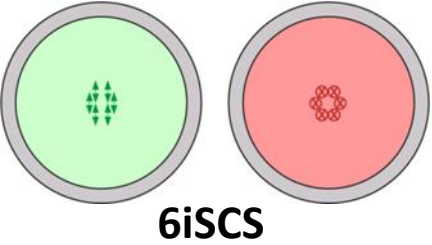
larger difference for 4iSCSS

-Purcell smaller: weaker resonance

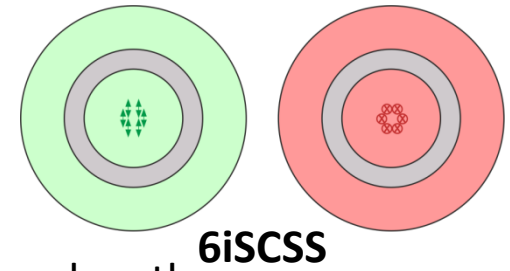
$-\delta R_{\text{exc}}$ larger (δR_{em} smaller): less efficient in emission enhancement

-smaller P_x & larger $P_x^* \text{cQE}$

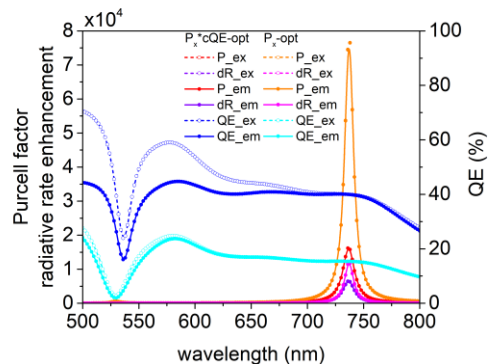
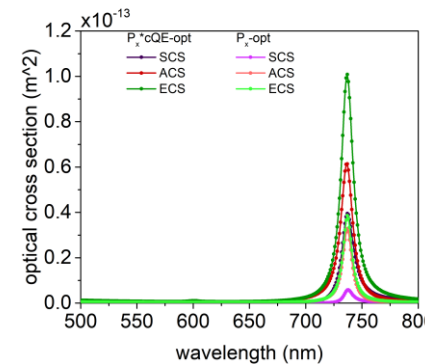
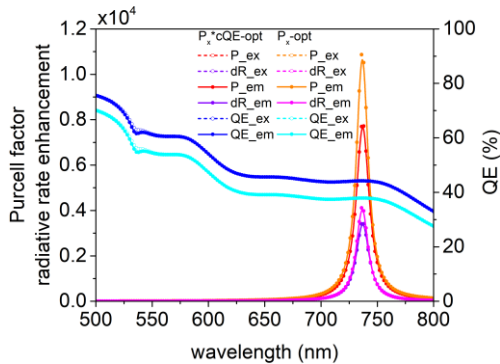
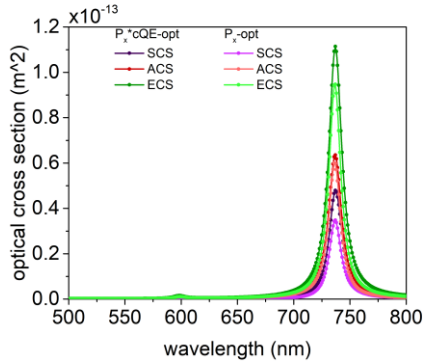
		P_{exc} (a.u.)	QE (%)	δR_{exc} (a.u.)	P_{em} (a.u.)	cQE(%)	δR_{em} (a.u.)	P_x (a.u.)	$P_x^* \text{cQE}$ (a.u.)	R (nm)	t (nm)	d (nm)	GAR (a.u.)
4iSCS	P_x	6.8	59.7	4.1	7027.8	38.5	2703.2	10954.3	4213.5	30.2	5.1	26.9	0.8566
	$P_x^* \text{cQE}$	6.4	66.3	4.2	5241.3	44.2	2316.1	9151.5	4309.6	32.6	5.5	29.4	0.8556
4iSCSS	P_x	46.7	16.1	7.5	53584.1	15.2	8156.6	61470.1	9357	11.7	5	9.1	0.7009
	$P_x^* \text{cQE}$	19.4	42.7	8.3	11208.9	39.6	4435.6	36641.8	14499.8	18.2	7.4	13.6	0.7123



$P_x \leftrightarrow P_x^* \text{cQE: right FOM}$



Single peak on the ecs, scs, Purcell, δR at the emission wavelength



$(I_{min}) I_{max}$ on QE at (exc) emission

$(g_{min}) \text{ plateau} / I_{max}$ on QE at (exc) emission
for $P_x / P_x^* \text{cQE}$

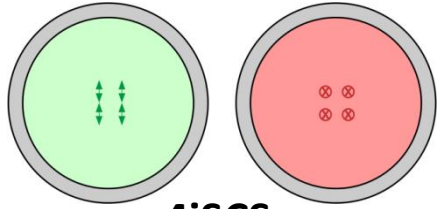
$P_x \leftrightarrow P_x^* \text{cQE - geometry}$

larger core, thicker shell, similar GAR,
larger dipole distance

$P_x \leftrightarrow P_x^* \text{cQE - optical response}$

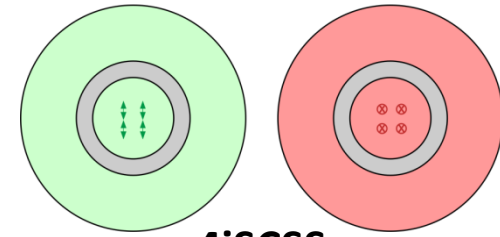
- QE larger
 - Purcell smaller: weaker resonance
 - δR_{exc} larger (δR_{em} smaller): less efficient in emission enhancement
 - smaller P_x & larger $P_x^* \text{cQE}$
- larger difference for 6iSCSS
6iSCSS larger cQE at emission than at excitation

		P_{exc} (a.u.)	QE (%)	δR_{exc} (a.u.)	P_{em} (a.u.)	cQE(%)	δR_{em} (a.u.)	P_x (a.u.)	$P_x^* \text{cQE}$ (a.u.)	R (nm)	t (nm)	d (nm)	GAR (a.u.)
6iSCS	P_x	10.3	58.8	6	10984.7	37.8	4151.7	25087.4	9481.8	30	5	26.5	0.8568
	$P_x^* \text{cQE}$	9.7	65	6.3	7871.1	44.2	3474.8	21989.5	9667.3	32.6	5.5	28.9	0.8555
6iSCSS	P_x	324.3	3.5	11.3	78999.7	15.4	12136.7	136649.7	20993.5	11.8	5	7.3	0.701
	$P_x^* \text{cQE}$	38	32.7	12.4	16386	39.9	6539.9	81311.4	32452.4	18.3	7.4	13	0.712



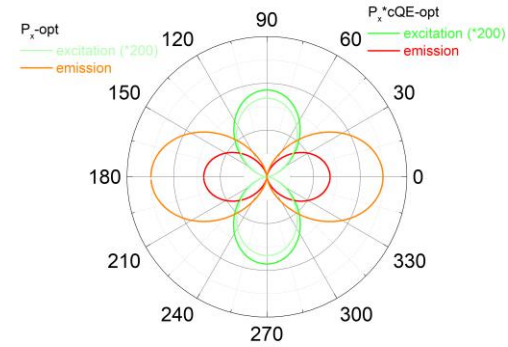
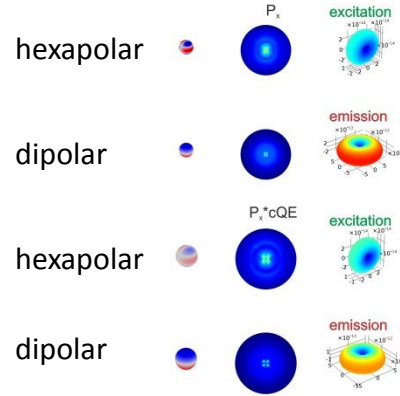
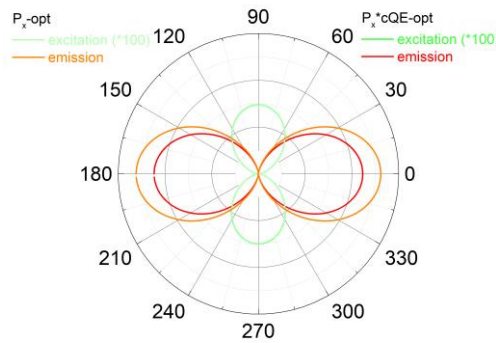
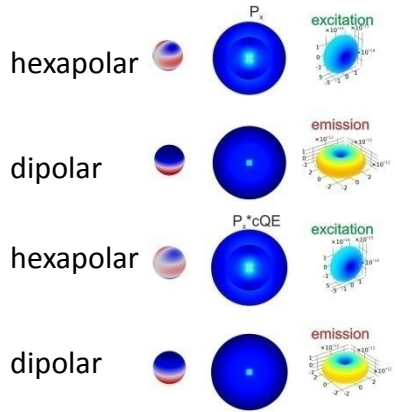
4iSCS

$$P_x \leftrightarrow P_x^* \text{cQE: right FOM}$$



4iSCSS

$exc \leftrightarrow em \sim 10^2$ *charge, Purcell factor, stronger resonance -> larger emission enhancement



$P_x \leftrightarrow P_x^* \text{cQE}$ – near- & far-field response

-smaller amount of accumulated charges according to weaker resonance

-larger (smaller) lobes at excitation (emission)

-FWHM larger -> Q factor smaller

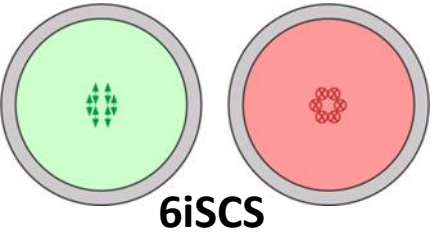
-bad cavity more well defined in 4iSCS

-detuning smaller in ecs

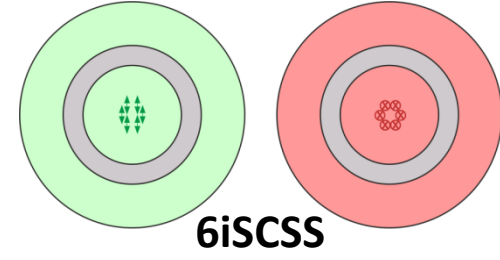
in 4iSCSS

-detuning smaller in Purcell & δR & scs

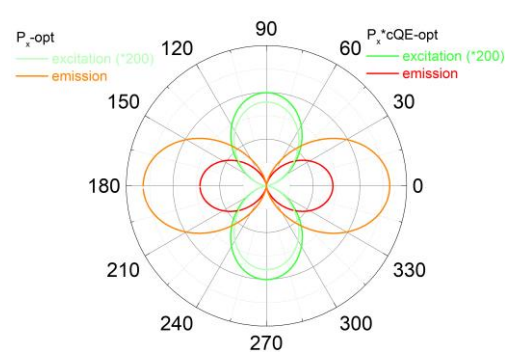
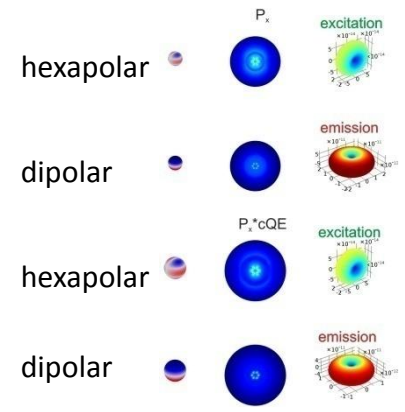
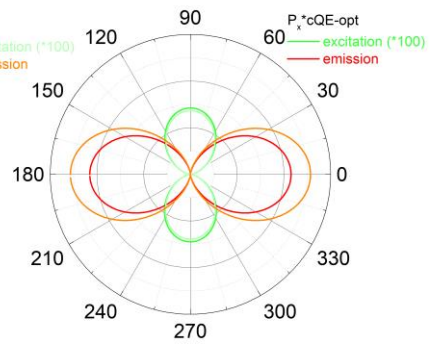
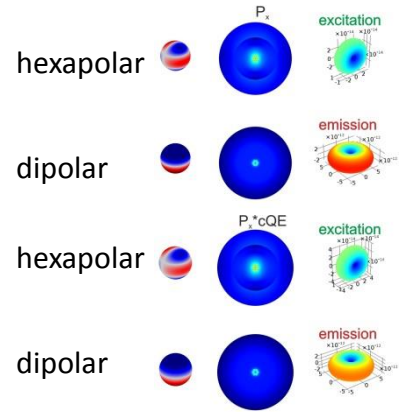
		charge (C)		FWHM (nm)				detuning (nm)				Q-factor (a.u.)	
		excitation	emission	Purcell	δR	ecs	scs	Purcell	δR	ecs	scs	Purcell	ecs
4iSCS	P_x	3.00E-16	5.25E-14	12.89	12.48	12.89	12.98	-0.21	-0.21	-0.34	0.60	58.71	57.13
	$P_x^* \text{cQE}$	2.29E-16	4.55E-14	14.04	13.62	14.04	14.13	0.27	0.26	0.22	0.65	53.89	52.49
4iSCSS	P_x	5.96E-15	3.40E-13	9.41	9.09	9.41	9.10	0.78	0.46	0.19	1.29	80.90	78.37
	$P_x^* \text{cQE}$	3.63E-15	1.57E-13	12.97	12.25	12.67	12.58	0.46	0.42	0.44	1.23	59.91	58.13



$$P_x \leftrightarrow P_x^* \text{cQE: right FOM}$$



$exc \leftrightarrow em \sim 10^2 * charge$ (except 6iSCSS_ P_x), Purcell factor, stronger resonance - > larger emission enhancement



$$P_x \leftrightarrow P_x^* \text{cQE near- \& far-field response}$$

exception: 6iSCS at excitation

- smaller amount of accumulated charges according to weaker resonance
- larger (smaller) lobes at excitation (emission)
- FWHM larger -> Q factor smaller

-bad cavity more well defined in 6iSCS

-detuning smaller in Purcell, δR , ecs

6iSCSS

-detuning smaller in ecs

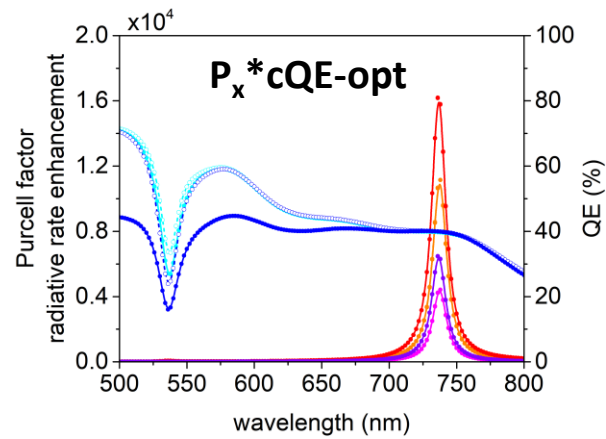
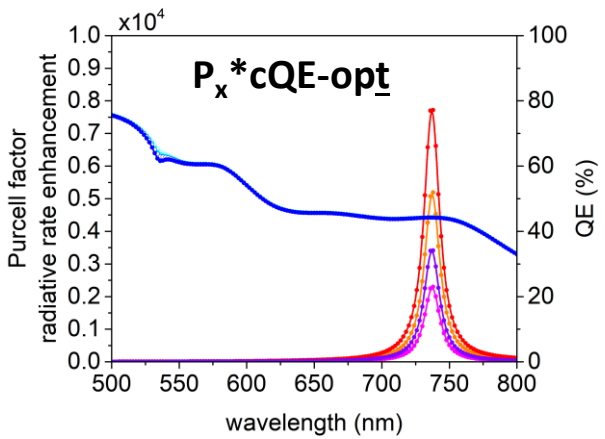
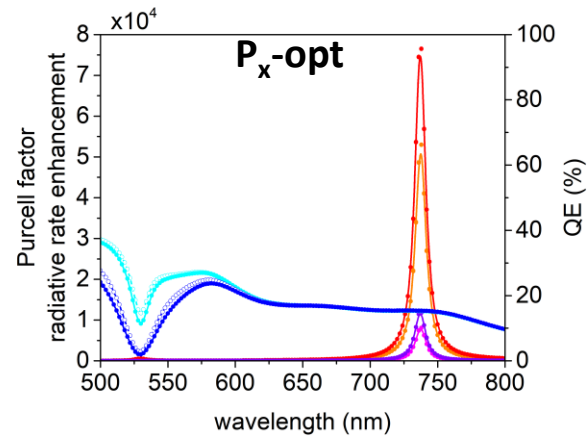
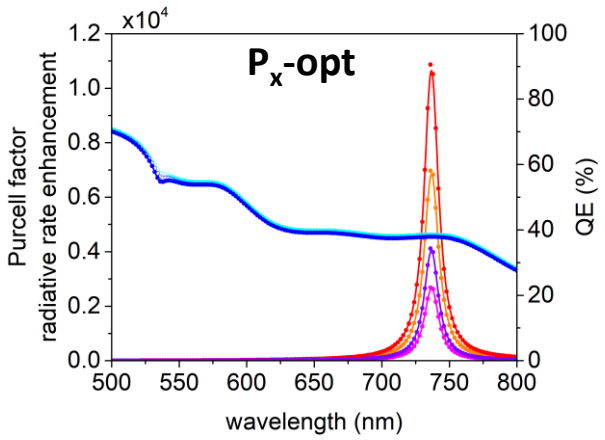
		charge (C)		FWHM (nm)				detuning (nm)				Q-factor (a.u.)	
		excitation	emission	Purcell	δR	ecs	scs	Purcell	δR	ecs	scs	Purcell	ecs
6iSCS	P_x	4.65E-16	8.06E-14	12.43	12.36	12.77	12.86	-0.03	-0.33	-0.39	0.01	59.29	57.66
	$P_x^* \text{cQE}$	4.83E-16	6.82E-14	13.68	13.62	14.04	14.14	0.02	0.01	0.03	0.46	53.88	52.48
6iSCSS	P_x	2.58E-14	5.07E-13	9.12	9.10	9.42	9.13	0.14	0.13	0.15	0.75	80.83	78.23
	$P_x^* \text{cQE}$	7.48E-15	2.32E-13	12.56	12.50	12.78	12.69	0.46	0.43	-0.05	1.24	58.71	57.68

4 ↔ 6 dipoles

6 ↔ 4

CS nanoresonator

CSS nanoresonator



- | | |
|---|--|
| 6 dipoles | 4 dipoles |
| —○— Purcell_ex | —○— Purcell_ex |
| —○— δR_{ex} | —○— δR_{ex} |
| —○— QE_ex | —○— QE_ex |
| — Purcell_em | — Purcell_em |
| — δR_{em} | — δR_{em} |
| — QE_em | — QE_em |

-core radius, shell thickness, GAR ~same (for same optimization), distance smaller

-QE smaller & same near λ_{exc} & λ_{em} except in SCSS at λ_{em}
 -larger Purcell factor & δR independently of the optimization
-larger P_x and $P_x * cQE$

-larger amount of accumulated charges
 -larger far-field lobes

-larger FWHM (9 exceptions)
 -smaller Q (2 exceptions)
-bad cavity more well defined
 -detuning smaller (5 exceptions)
 - Δf difference smaller (same) in SCSS (SCSS)

CS ↔ CSS

SCSS ↔ SCS

4 dipoles

6 dipoles

-larger core, thinner shell
(e: 4iCS&CSS_P_x) => larger GAR, larger distance

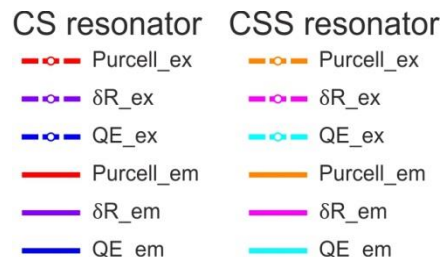
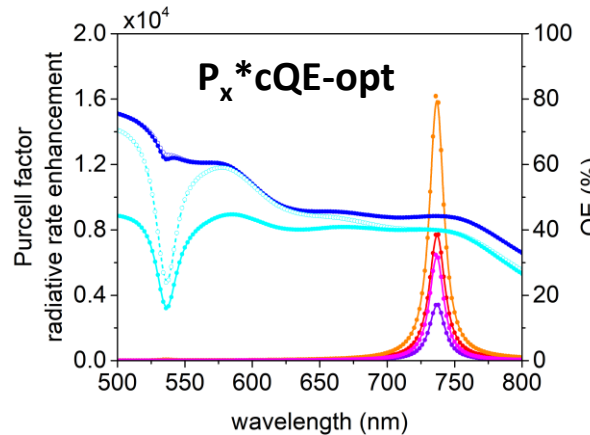
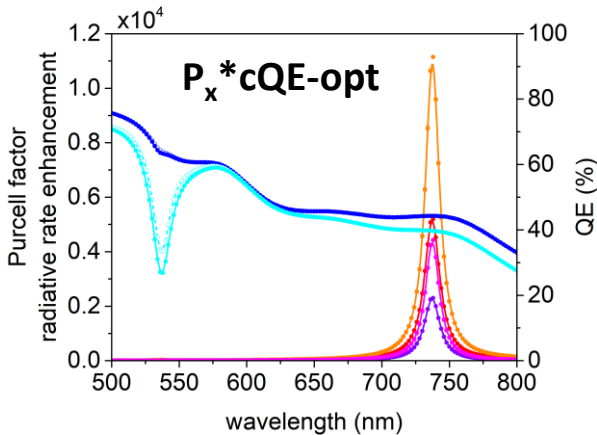
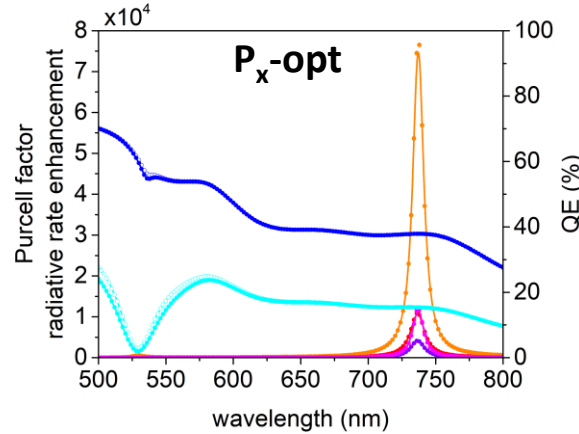
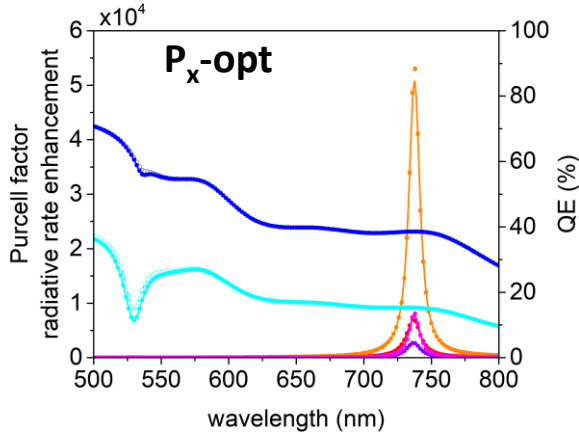
-QE larger
(more with P_x objective function)
-smaller Purcell & δR at exc & em
-smaller P_x and P_x*cQE

-weaker charge accumulation
-smaller far-field lobes

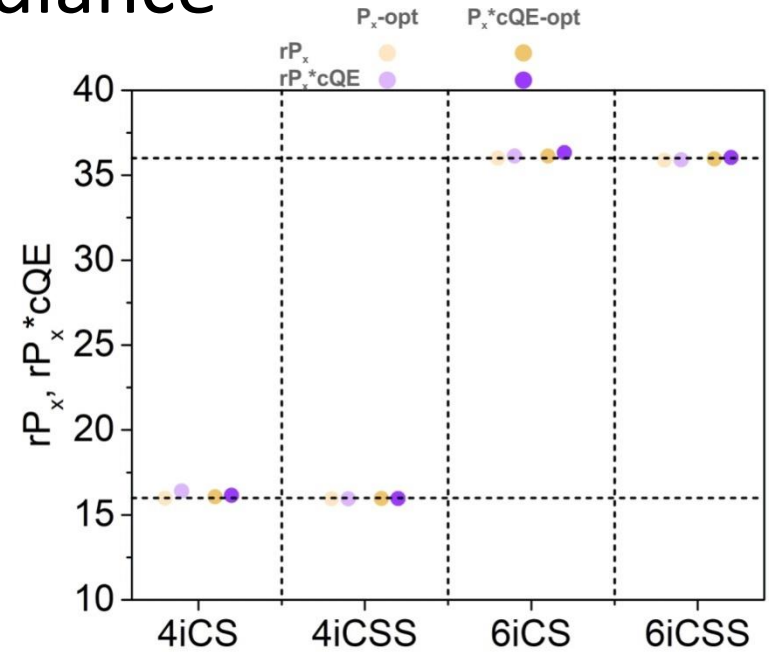
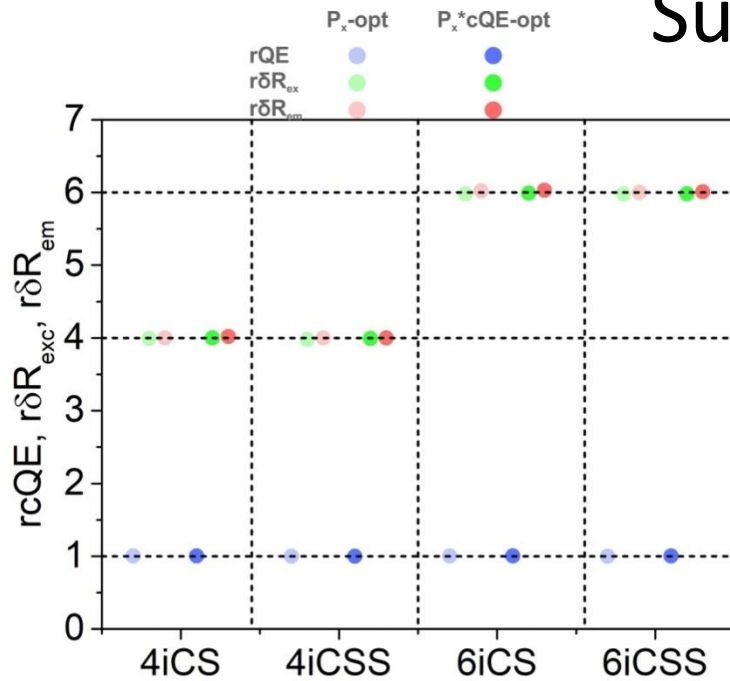
-larger FWHM, smaller Q
-bad cavity better in SCS

-detuning is smaller in SCS
3 exceptions: in ecs for 4iSCS_P_x
in δR and ecs for 6iSCS_P_x

-difference in Δf is smaller in SCS



Superradiance



$P_x \leftrightarrow P_x^*cQE$ (17/20): better for δR_{exc} & δR_{em} & rcQE & P_x & P_x^*cQE (e: $r\delta R_{em}$, rcQE in 4iCSS; δR_{exc} in 6iCSS)

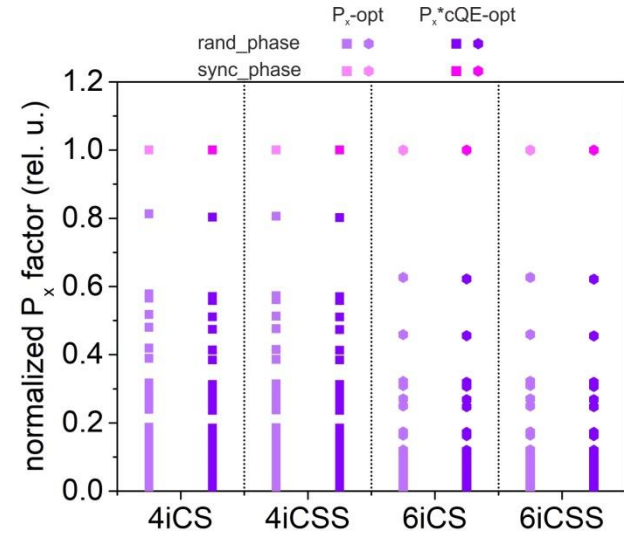
4 \leftrightarrow 6 (13/30): better for $r\delta R_{exc}$ in 6iSCSS_ P_x , $r\delta R_{em}$ & rP_x in 6iSCS_ P_x , 6iSCSS_ P_x^*cQE , rP_x^*cQE in 6iSCS_ P_x , 6iSCSS_ P_x & P_x^*cQE

CS \leftrightarrow CSS (22/30): better for $r\delta R_{exc}$ & $r\delta R_{em}$ & rcQE & rP_x & rP_x^*cQE

(e: $r\delta R_{exc}$ in 6iCS_ P_x , $r\delta R_{em}$ in 4iCS_ P 6iCS_ P_x) on the average for all SCS

	4iCS		4iCSS		6iCS		6iCSS	
	P_x -opt	P_x^*cQE -opt	P_x -opt	P_x^*cQE -opt	P_x -opt	P_x^*cQE -opt	P_x -opt	P_x^*cQE -opt
$r\delta R_{exc}$	3.99	4	3.98	3.99	5.98	5.99	5.98	5.98
$r\delta R_{em}$	4.01	4.02	4.01	4	6.02	6.03	6	6.01
rcQE	1.0031	1.005	1	0.9994	1.0033	1.0055	1.0008	1.0025
rP_x	15.99	16.07	15.95	15.97	36	36.13	35.88	35.95
rP_x^*cQE	16.04	16.15	15.95	15.96	36.12	36.33	35.91	36.04
$\bar{\Sigma}_r$ average	5.003	5.018	4.992	4.994	4.996	5.026	4.991	4.999

Comparison of collective and random systems

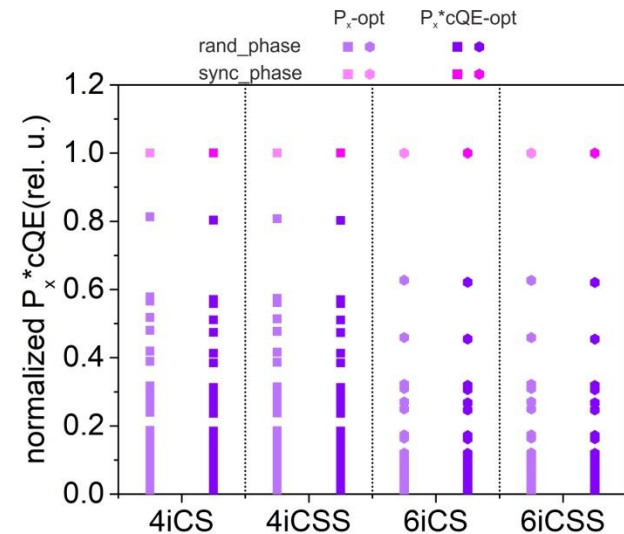


-larger P_x & P_x *cQE in collectively oscillating systems

- P_x *cQE (P_x) is larger in systems optimized with P_x *cQE (P_x) objective function

-more significant difference for **6** dipoles (independently of the optimization or the resonator type)

- P_x and P_x *cQE is larger in nanoresonators consisting of **6 dipoles** independently of the optimization



- P_x and P_x *cQE is larger in **SCSS** type nanoresonators, independently of the optimization

- P_x objective function to improve non-cooperative emission

- **P_x *cQE objective function to improve cooperative emission**

Distance dependency of Purcell factor

$$\frac{\text{splitting}_{max}}{\langle Purcell_{max}, Purcell_{min} \rangle}$$

excitation

emission

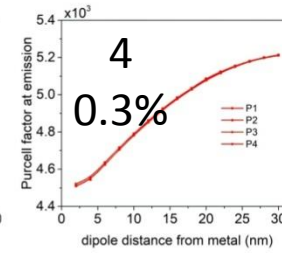
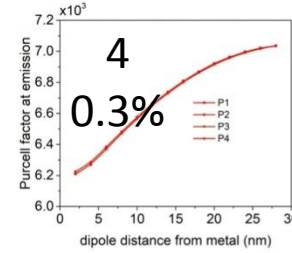
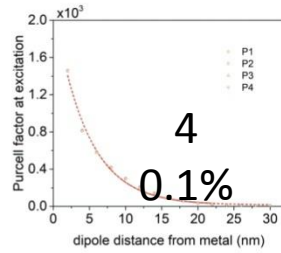
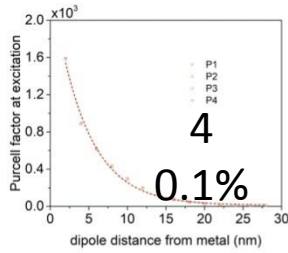
P_x -opt

P_x^* cQE-opt

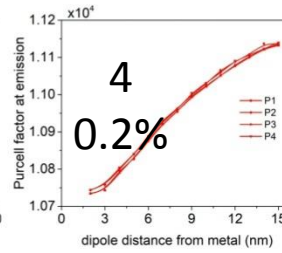
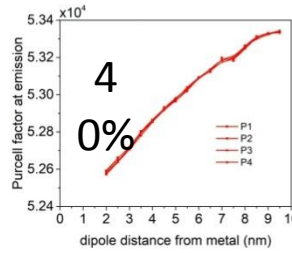
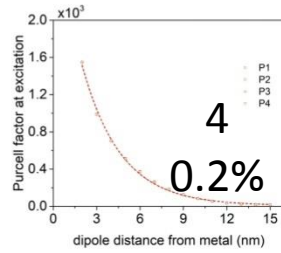
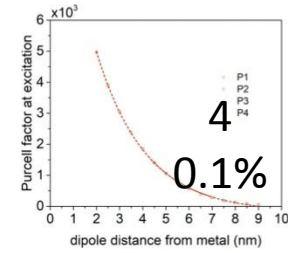
P_x -opt

P_x^* cQE-opt

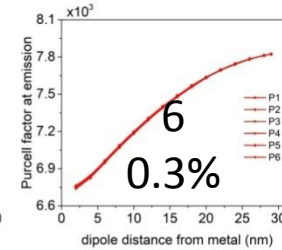
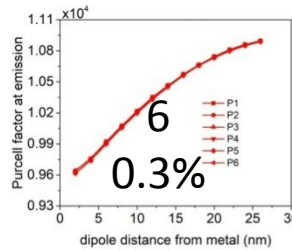
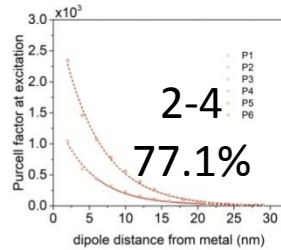
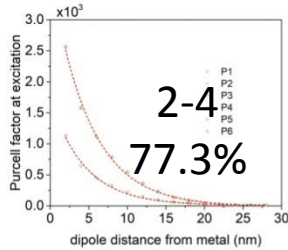
4iCS



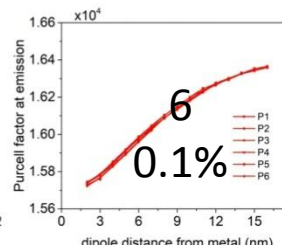
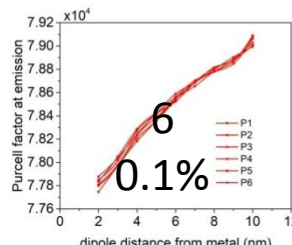
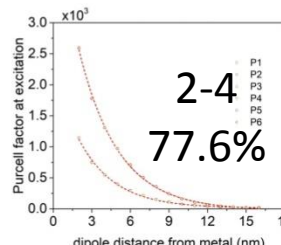
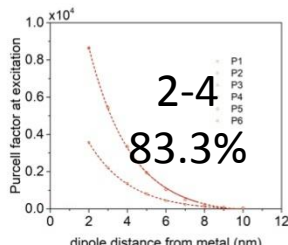
4iCCS



6iCS



6iCCS



Conclusion

- $P_x / P_x^* \text{cQE}$ efficient to maximize non-cooperative / **cooperative** fluorescence
 P_x & $P_x^* \text{cQE}$ is larger in case of 6 dipoles and SCSS type resonators
average ratio larger/smaller for 6 dipoles for SCS & SCSS in case of $P_x^* \text{cQE} / P_x$
- 4 / 6 larger seeding is more suitable to result in **non-cooperative & cooperative** fluorescence
FWHM is larger \rightarrow the Q factor is smaller, and $\Delta\lambda$ is smaller
- SCSS / **SCS** type resonators are more suitable for non-cooperative / **cooperative** fluorescence
FWHM is larger \rightarrow the Q factor is smaller, and $\Delta\lambda$ is smaller in **SCS** type nanoresonators
- line-width narrowing
- indistinguishable: both configurations in case of 4 dipoles (proposed 4iSCS)
- δR & far-field: 4iSCS-4iSCSS-6iSCS-6iSCSS
- ranking of P_x spherical nanoresonators: 4iSCSS < 4iSCS = 6iSCS < 6iSCSS
- ranking of $P_x^* \text{cQE}$ spherical nanoresonators: **4iSCSS < 4iSCS < 6iSCSS < 6iSCS**
- **proposed: 6iSCS: larger efficiency, smaller detuning and deviation in frequency pulling**

Acknowledgements

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