

FEM Based Design and Simulation Tool for MRI Birdcage Coils Including Eigenfrequency Analysis

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Outline

- 1 Introduction
 - RF coils in MRI
 - RF birdcage coils
 - Design and simulation of RF birdcage coils
- 2 Motivation
 - Review of previous studies
 - Problem definition
 - Our work
- 3 Methods
 - FEM Models of Birdcage Coils
 - Frequency Domain Analysis
 - Eigenfrequency Analysis
 - Software Tool
- 4 Experimental Results
- 5 Conclusion

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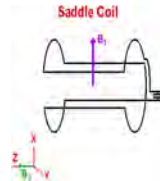
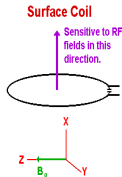
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What Do the RF Coils Serve in MRI?

- generate RF magnetic field (B_1 field) at the Larmor frequency
- receive RF signals at the same frequency



Source of figures: <http://www.cis.rit.edu/htbooks/mri/chap-9/chap-9.htm>

RF Birdcage Head Coil Example



Source of figure: <http://www.healthcare.philips.com>

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RF birdcage coils

Design and simulation of RF birdcage coils

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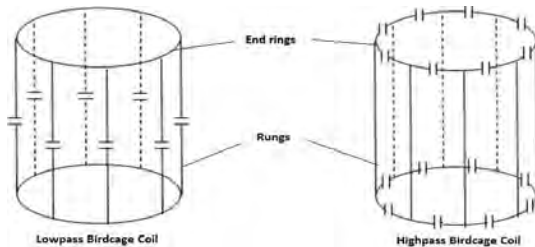
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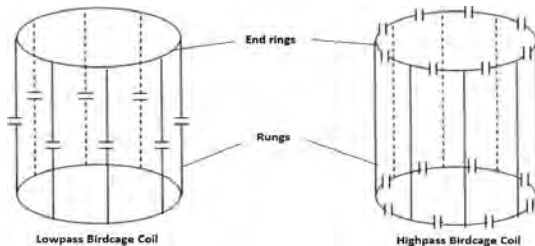
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Birdcage Coils Consist of...



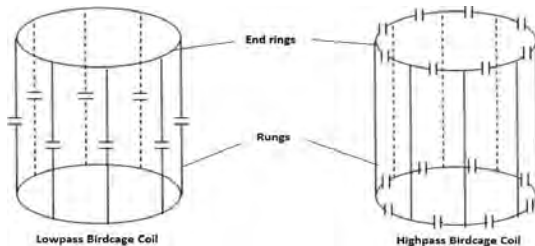
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- two circular end rings connected by N equally spaced rungs (or legs)



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- capacitors on the rungs or end rings or both



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A birdcage coil with N number of rungs and equal valued capacitors has

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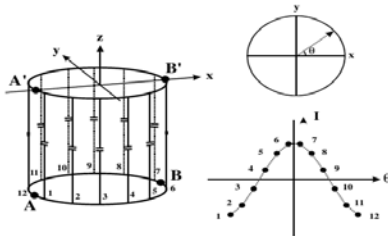
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 - currents only flow in the end rings - Helmholtz pair

Which Resonant Mode is used in MRI?

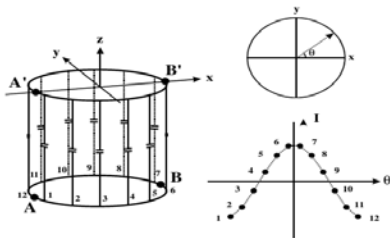
- most homogeneous B_1 field
- sinusoidal current distribution in the rungs for $m = 1$ mode



Source of figure: M. Lupu, MAGMA, 2004, 17, 363-371

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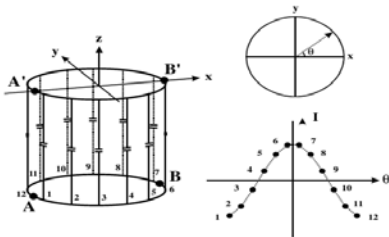
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Designing a RF Birdcage Coil

In order to generate a homogeneous B_1 field at the desired frequency;

- use the correct capacitance value
 - calculate an initial capacitance value
 - tuning and matching procedures
- knowing resonant modes of the birdcage coil
 - tuning and matching procedures can be done without interfering with the other modes
 - $m=0$ mode is used in open MRI systems

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Simulating a RF Birdcage Coil

Solving for the electromagnetic fields of a birdcage coil at the specified frequency.

- B_1 field distribution inside the coil
- specific absorption rate (SAR) at any object
- variation of any electromagnetic field variables with respect to frequency

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Studies on Designing a Birdcage Coil

Tropp, 1989

analyzing low-pass birdcage resonator - using lumped circuit element model and perturbation theory

Jin, 1989

resonant modes calculation - lumped circuit element model

Pascone et al., 1991

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Lumped Circuit Element Model

- end rings and rungs are modeled as inductors
- self and mutual inductances are calculated using handbook formulas
- equivalent circuit model (LC network) is solved using Kirchoff's voltage and current laws

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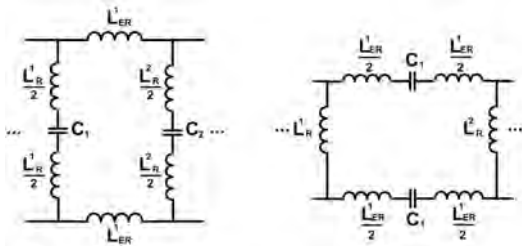
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Figure: Equivalent lumped circuit element models for low-pass and high-pass birdcage coils



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Modelling a Transmission Line as a Lumped Circuit Element

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$$\text{length of wire} \leq \frac{\lambda}{20}$$

where λ is the wavelength.

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A handmade low-pass birdcage coil is constructed.

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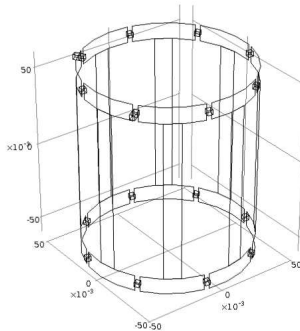
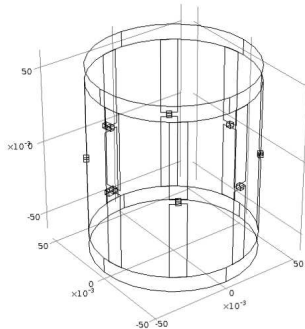
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- low-pass and high-pass birdcage coils are geometrically modeled in the simulation environment

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Frequency Domain Analysis

Eigenfrequency Analysis

Software Tool

Adding Physics

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- Radio Frequency Branch → Electromagnetic Waves Interface

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$$\nabla \times \mu_r^{-1}(\nabla \times \mathbf{E}) - k_0^2 \left(\epsilon_r - \frac{j\sigma}{\omega\epsilon_0} \right) \mathbf{E} = 0$$

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Boundary Conditions

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- boundaries of rungs, end rings, capacitor plates and RF shield are assigned to **Perfect Electric Conductor (PEC)**

Boundary Conditions

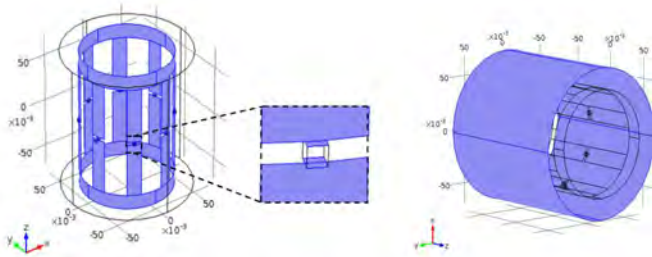
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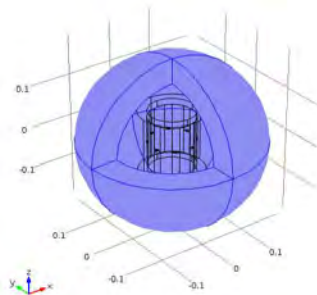
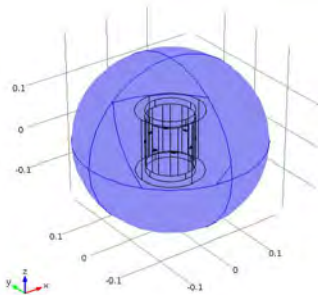
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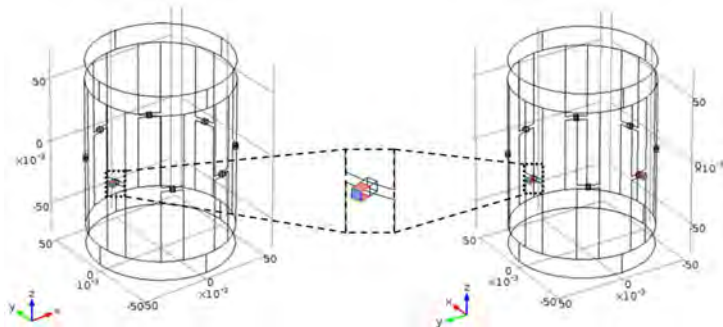
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- In frequency domain analysis, **lumped port boundary condition** is used for voltage excitation ($Z_{port} = \frac{V_{port}}{I_{port}}$)

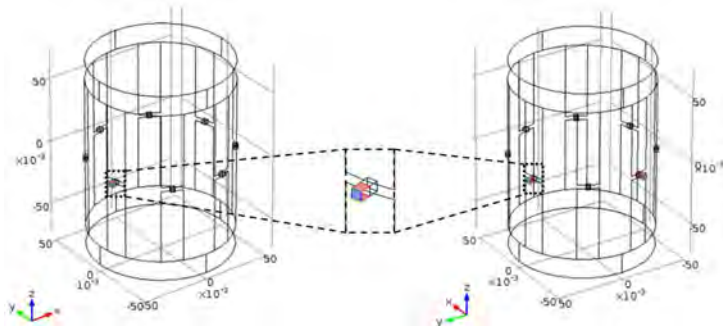
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- In eigenfrequency analysis, no source is applied

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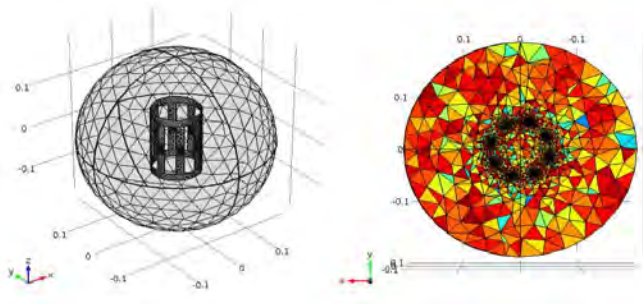
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In Frequency Domain Analysis;

- loaded (or unloaded) birdcage coils
- shielded (or unshielded) birdcage coils
- linear or quadrature excitation

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FEM Models of Birdcage Coils

Frequency Domain Analysis

Eigenfrequency Analysis

Software Tool

Simulation Results

Simulation Results

three different scenarios;

Simulation Results

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- unloaded and unshielded 8-leg low-pass birdcage coil

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- H^+ and H^-

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$$H^+ = \frac{H_x + iH_y}{2} \quad H^- = \frac{(H_x - iH_y)^*}{2}$$

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- E-field

Simulation Results - 1st Scenario

Unloaded and Unshielded 8-leg Low-pass BC

Simulation Results - 1st Scenario

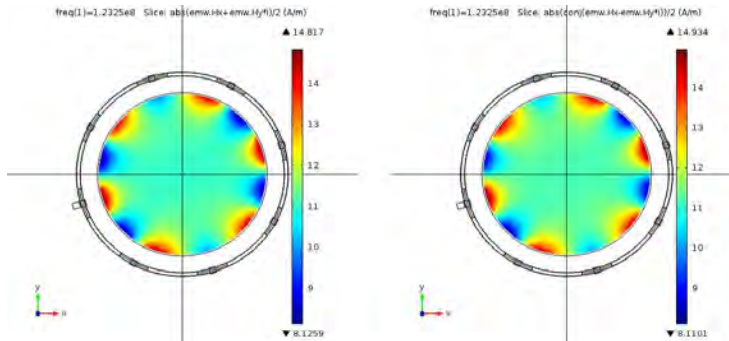
Unloaded and Unshielded 8-leg Low-pass BC

\mathbf{H}^+ and $\mathbf{H}^- \rightarrow$ for linear excitation

Simulation Results - 1st Scenario

Unloaded and Unshielded 8-leg Low-pass BC

H^+ and $H^- \rightarrow$ for linear excitation



Simulation Results - 1st Scenario

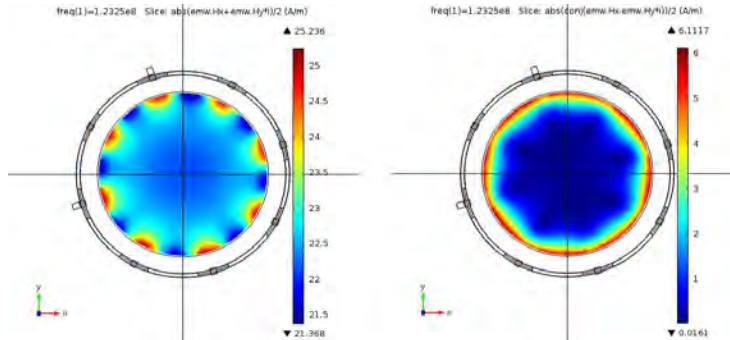
Unloaded and Unshielded 8-leg Low-pass BC

\mathbf{H}^+ and $\mathbf{H}^- \rightarrow$ for quadrature excitation

Simulation Results - 1st Scenario

Unloaded and Unshielded 8-leg Low-pass BC

H^+ and $H^- \rightarrow$ for quadrature excitation



Simulation Results - 1st Scenario

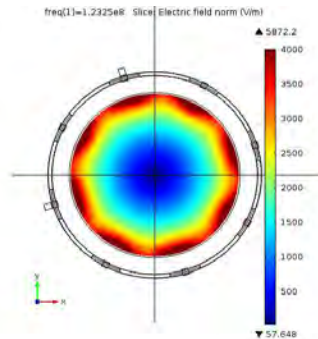
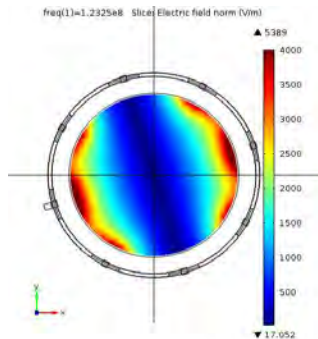
Unloaded and Unshielded 8-leg Low-pass BC

Electric field → for linear and quadrature excitation

Simulation Results - 1st Scenario

Unloaded and Unshielded 8-leg Low-pass BC

Electric field → for linear and quadrature excitation



Simulation Results - 1st Scenario

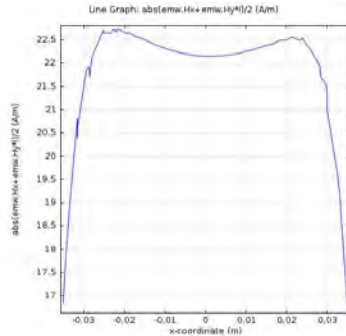
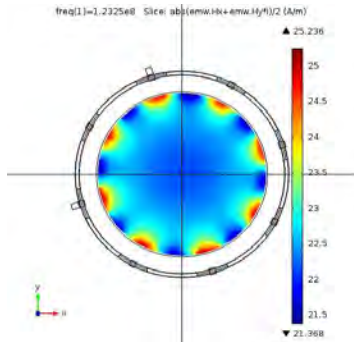
Unloaded and Unshielded 8-leg Low-pass BC

H⁺ uniformity → for quadrature excitation

Simulation Results - 1st Scenario

Unloaded and Unshielded 8-leg Low-pass BC

H⁺ uniformity → for quadrature excitation



Simulation Results - 2nd Scenario

Unloaded and Shielded 8-leg Low-pass BC

Simulation Results - 2nd Scenario

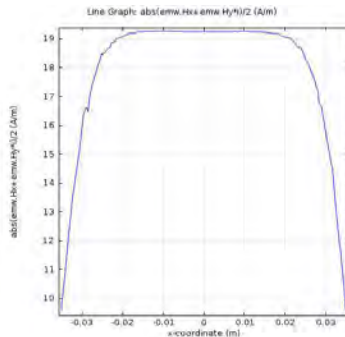
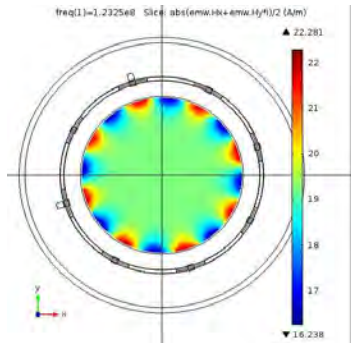
Unloaded and Shielded 8-leg Low-pass BC

H⁺ uniformity → for quadrature excitation

Simulation Results - 2nd Scenario

Unloaded and Shielded 8-leg Low-pass BC

H^+ uniformity \rightarrow for quadrature excitation



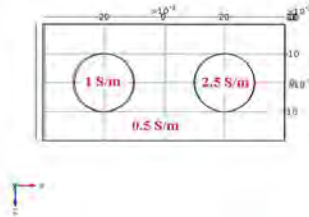
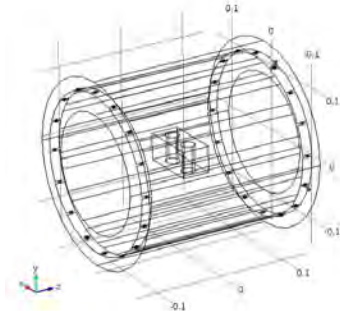
Simulation Results - 3rd Scenario

Loaded and Shielded 16-leg High-pass BC

Simulation Results - 3rd Scenario

Loaded and Shielded 16-leg High-pass BC

Geometric model



Simulation Results - 3rd Scenario

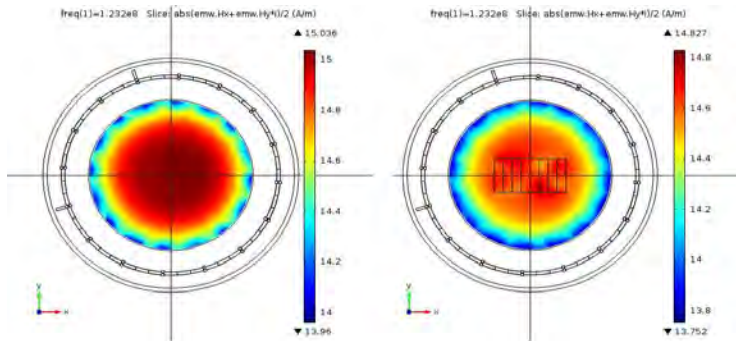
Loaded and Shielded 16-leg High-pass BC

\mathbf{H}^+ → for unloaded and loaded case (quadrature excitation)

Simulation Results - 3rd Scenario

Loaded and Shielded 16-leg High-pass BC

H^+ → for unloaded and loaded case (quadrature excitation)



Simulation Results - 3rd Scenario

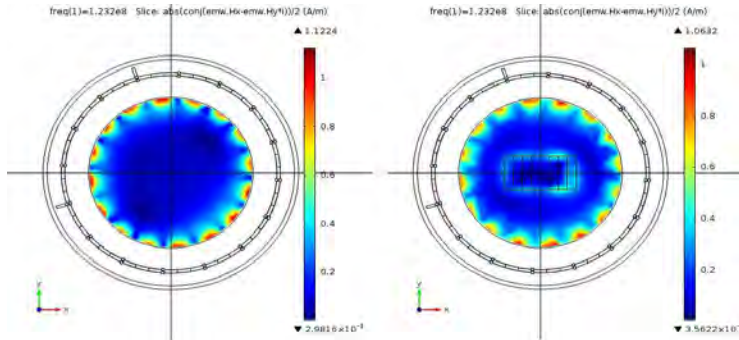
Loaded and Shielded 16-leg High-pass BC

H^- → for unloaded and loaded case (quadrature excitation)

Simulation Results - 3rd Scenario

Loaded and Shielded 16-leg High-pass BC

$H^- \rightarrow$ for unloaded and loaded case (quadrature excitation)



Simulation Results - 3rd Scenario

Loaded and Shielded 16-leg High-pass BC

SAR distribution of an object

Simulation Results - 3rd Scenario

Loaded and Shielded 16-leg High-pass BC

SAR distribution of an object

$$SAR = \frac{\sigma |\mathbf{E}|^2}{\rho}$$

σ : conductivity, ρ : density

Simulation Results - 3rd Scenario

Loaded and Shielded 16-leg High-pass BC

SAR distribution of an object

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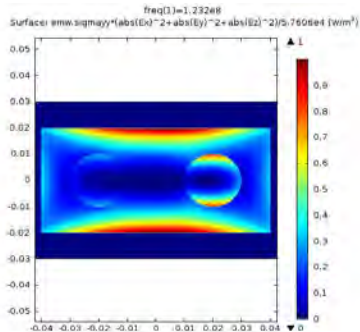
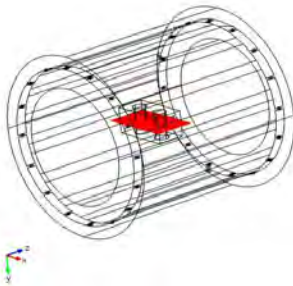
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Normalized SAR distribution → for quadrature excitation

Simulation Results - 3rd Scenario

Loaded and Shielded 16-leg High-pass BC

Normalized SAR distribution → for quadrature excitation



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Resonant Mode Analysis of a Birdcage Coil

Resonant Mode Analysis of a Birdcage Coil

calculates the resonant modes of the birdcage coil

Resonant Mode Analysis of a Birdcage Coil

calculates the resonant modes of the birdcage coil **and the electromagnetic field distributions at these resonant modes**

Resonant Mode Analysis of a Birdcage Coil

calculates the resonant modes of the birdcage coil **and the electromagnetic field distributions at these resonant modes** for the given capacitance value

Eigenfrequency Analysis in COMSOL Multiphysics

Eigenfrequency Analysis in COMSOL Multiphysics

- use developed FEM models of birdcage coils

Eigenfrequency Analysis in COMSOL Multiphysics

- use developed FEM models of birdcage coils
- add eigenfrequency study

Eigenfrequency Analysis in COMSOL Multiphysics

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 - specify number of eigenfrequencies

Eigenfrequency Analysis in COMSOL Multiphysics

- use developed FEM models of birdcage coils
- add eigenfrequency study
 - specify number of eigenfrequencies
 - specify a frequency point
- add eigenvalue solver

Eigenfrequency Analysis in COMSOL Multiphysics

- use developed FEM models of birdcage coils
- add eigenfrequency study
 - specify number of eigenfrequencies
 - specify a frequency point
- add eigenvalue solver
 - change the linearization point (if necessary)

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- H^+ at these resonant modes

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observed electromagnetic variables

- H^+ at these resonant modes
- surface current density

Simulation Results - 1st Scenario

Unloaded and Unshielded 8-leg Low-pass BC

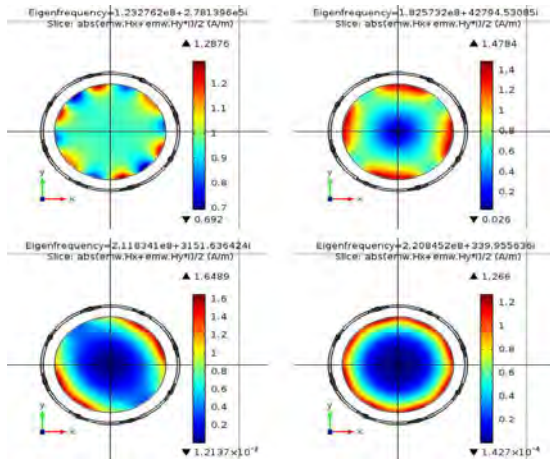
Simulation Results - 1st Scenario

Unloaded and Unshielded 8-leg Low-pass BC

\mathbf{H}^+ → for all resonant modes

Simulation Results - 1st Scenario

Unloaded and Unshielded 8-leg Low-pass BC



Simulation Results - 2nd Scenario

Unloaded and shielded 16-leg High-pass BC

Simulation Results - 2nd Scenario

Unloaded and shielded 16-leg High-pass BC

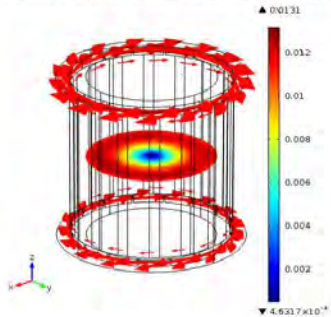
H^+ and surface current densities → for $m=0$ mode

Simulation Results - 2nd Scenario

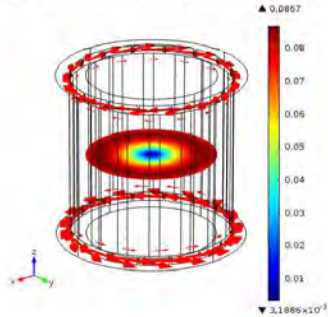
Unloaded and shielded 16-leg High-pass BC

H^+ and surface current densities \rightarrow for $m=0$ mode

Arrow Surface: Surface current density Slice: $\text{abs}(\text{emw.Hx} + \text{emw.Hy}^2)/2$ (A/m)



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Software Tool for Designing and Simulating a Birdcage Coil

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PURPOSE:

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- To provide convenience for the coil designers and the researchers in the field of MRI

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developed software tool

- FEM based Frequency Domain and Eigenfrequency Analysis Tool (FEM-FDA-EFAT)

Properties of the software tool

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- developed in MATLAB

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- has graphical-user-interface (GUI)

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 - modeling the coil geometry
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 - generating mesh for the model
 - adding study and solver sequence
 - computing the solutions
- when the computation is finished, results can be observed in COMSOL Multiphysics

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Frequency Domain Analysis

Eigenfrequency Analysis

Software Tool

FEM-FDA-EFAT

FEM-FDA-EFAT

Circular Birdcage Coil v4.0

Design and Simulate

Default Values

Design Parameters

Type
 Lowpass Highpass

Number of legs (rungs)
 8 12 16 20 24

Coil radius meter

Leg width meter

Leg length meter

End ring width meter

End ring length meter

Desired resonance frequency Hz

RF shield radius meter

Design

Simulation Parameters

Study
 Frequency Domain Analysis Eigenfrequency Analysis

Start frequency Hz

Stop frequency Hz

Step frequency Hz

Number of freq.

Search freq. Hz

Domain/Boundary Condition
 Perfectly Matched Layer
 Scattering Boundary Condition

Excitation
 Linear Quadrature

Mesh
Mesh Size

Simulate

Results

Capacitor Value
 Use calculated capacitor value F
 Use different capacitor value F

Simulation is finished.

Elapsed time: 229.867 seconds

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Handmade Low-pass Birdcage Coil

Handmade Low-pass Birdcage Coil

- 8-leg low-pass birdcage coil is constructed on plexiglass tube

Handmade Low-pass Birdcage Coil



Experimental Results and Comparison with Numerical Analyses

for the resonant modes

Experimental Results and Comparison with Numerical Analyses

for the resonant modes

Experimental Results and Comparison with Numerical Analyses

for the resonant modes

- S_{11} of the coil for five different capacitance values

Experimental Results and Comparison with Numerical Analyses

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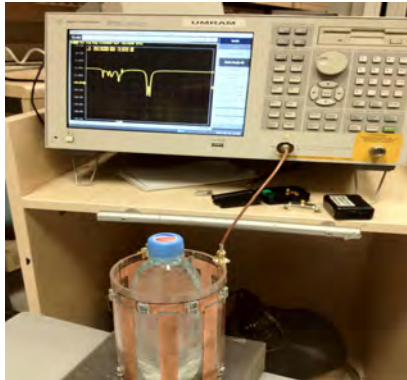
Experimental Results and Comparison with Numerical Analyses

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Experimental Results and Comparison with Numerical Analyses

Experimental Results and Comparison with Numerical Analyses



Measured and Calculated Resonant Modes Results for Low-pass Birdcage Coil

Measured and Calculated Resonant Modes Results for Low-pass Birdcage Coil

used capacitance values

47 pF, 10 pF, 3.3 pF, 1.8 pF, 1 pF

Measured and Calculated Resonant Modes Results for Low-pass Birdcage Coil

Results for 47pF

Modes	Measured (MHz)	MRIEM (MHz)	FEM-EFAT (MHz)
m=1	60.75	67.46	59.1
m=2	85.88	90.64	87.22
m=3	93.38	102.2	101.1
m=4	102.8	-	105.4

Measured and Calculated Resonant Modes Results for Low-pass Birdcage Coil

Results for 10pF

Modes	Measured (MHz)	MRIEM (MHz)	FEM-EFAT (MHz)
m=1	122.11	146.25	124.76
m=2	196.48	196.51	184.80
m=3	208.54	221.57	214.41
m=4	214.97	-	223.54

Measured and Calculated Resonant Modes Results for Low-pass Birdcage Coil

Results for 3.3pF

Modes	Measured (MHz)	MRIEM (MHz)	FEM-EFAT (MHz)
m=1	211.3	254.59	205.37
m=2	306.3	342.08	306.62
m=3	330.0	385.71	356.47
m=4	345.0	-	371.75

Measured and Calculated Resonant Modes Results for Low-pass Birdcage Coil

Results for 1.8pF

Modes	Measured (MHz)	MRIEM (MHz)	FEM-EFAT (MHz)
m=1	255.2	344.71	260.62
m=2	382.0	463.19	392.18
m=3	417.0	522.26	456.8
m=4	441.5	-	476.5

Measured and Calculated Resonant Modes Results for Low-pass Birdcage Coil

Results for 1pF

Modes	Measured (MHz)	MRIEM (MHz)	FEM-EFAT (MHz)
m=1	335.7	462.48	316.85
m=2	473.1	621.42	481.6
m=3	512.3	700.68	562.24
m=4	525.9	-	586.63

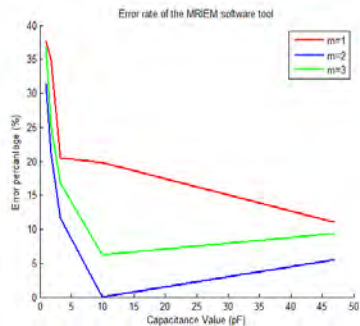
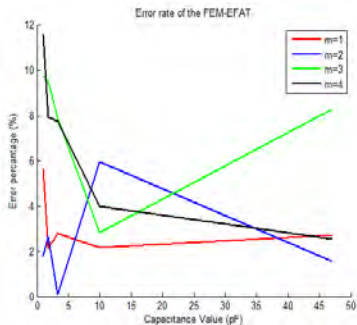
Measured and Calculated Resonant Modes Results for Low-pass Birdcage Coil

Percentage error

$$\text{Error rate (\%)} = 100 \times \left| \frac{f_{meas} - f_{calc}}{f_{meas}} \right|$$

Measured and Calculated Resonant Modes Results for Low-pass Birdcage Coil

Percentage error rate for FEM-EFAT and MRIEM



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We have proposed **two FEM based simulation methods** using **developed FEM models of low-pass and high-pass birdcage coils** in COMSOL Multiphysics:

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 - electromagnetic fields solutions of a birdcage coil for any scenario

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- **Frequency Domain Analysis**
 - electromagnetic fields solutions of a birdcage coil for any scenario
- **Eigenfrequency Analysis**
 - resonant modes of a birdcage coil and electromagnetic field solutions at these resonant modes

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- A software tool is developed to make these two simulation methods easily and according to the user-specified parameters
- Experimental results show that results of the proposed software tool is more accurate than the results of software tool which uses lumped circuit element model
- These methods can be adapted to design and simulate other MRI RF coils

One more thing...

One more thing...

Thank
you