

A THERMO ELASTIC MODEL FOR MICROWAVE ABLATION OF CONCRETE

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OUTLINE



- Microwave ablation of concrete surface (explosive spalling from high thermal stress and pore pressure from water vaporization)
- Material properties
- thermo elastic model with microwave heating
- Results simulation
- Experimental findings
- Conclusion

MATERIAL PROPERTIES, CONSTITUTIVE LAWS

ϵ_r	ρ [kg/m ³]	k [W/(m.K)]	C_p [J/(kg.K)]	ν	E [GPa]	α
6 - 0.5j	2400	1.7	800	0.12	48	10 ⁻⁵

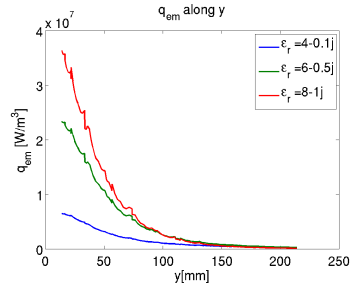
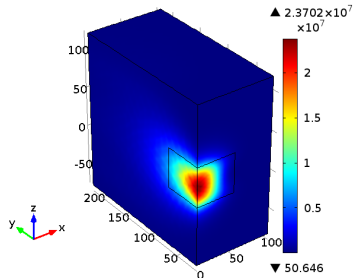
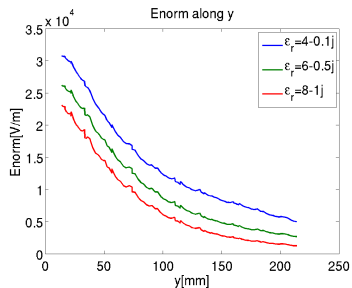
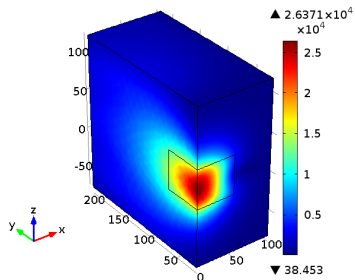
- in reality the materials properties vary with the water content and temperature
- electromagnetic losses: $P_{em} = \omega \epsilon_0 \epsilon'' E_{rms}^2$
- Assume isotropic and homogeneous material, electromagnetic part, $\mathbf{D} = \epsilon \mathbf{E}$
- thermal part: Fourier law, $\mathbf{q}(\mathbf{x}, t) = -k \nabla T(\mathbf{x}, t)$
- mechanical part: linear elastic model, $\sigma = E \epsilon$
- assume constant dielectric, thermal and mechanical properties
- linear thermo elastic model (generalized 3d hooke law)

$$\sigma = \frac{E}{1+\nu} \epsilon + \frac{E\nu}{(1+\nu)(1-2\nu)} \text{tr}(\epsilon) \mathbf{I} - \alpha \frac{E}{1-2\nu} (T - T_{ref}) \mathbf{I}$$

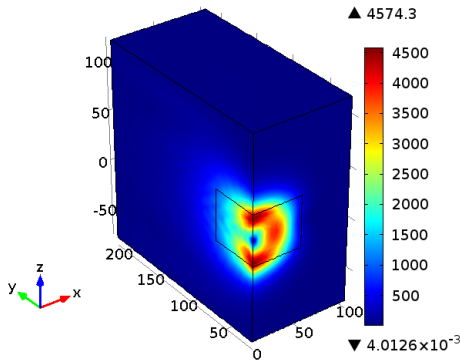
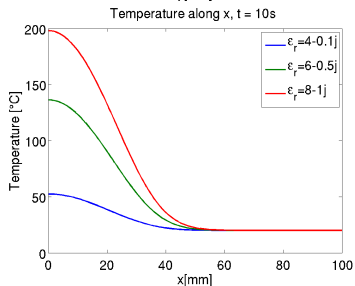
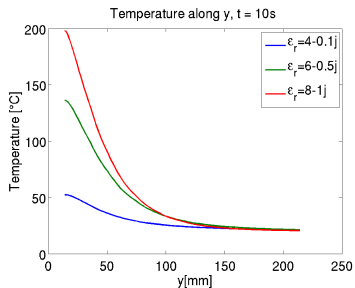
EM, THERMAL AND MECHANICAL MODELS

- EM: $\nabla^2 \mathbf{E} + \gamma^2 \mathbf{E} = 0$; $f = 2.45 \text{ GHz}$; $P_{in} = \frac{10}{2} \text{ kW}$
BC: boundary conditions, symmetry plane $\nabla \times \mathbf{H} = 0$, waveguide, $\mathbf{n} \times \mathbf{E} = 0$
concrete surface: radiation boundary condition
- THER: $\rho c_p \frac{\partial T(\mathbf{x}, t)}{\partial t} = \nabla \cdot (k \nabla T(\mathbf{x}, t)) + q_{em}(\mathbf{x}, t)$
 $T_i = 20 \text{ }^\circ\text{C}$; solve from 0 to 30 s every 2s
BC: $\mathbf{n} \cdot \nabla T = 0$
- MEC: $\rho \ddot{\mathbf{u}}(\mathbf{x}, t) - \nabla \cdot \mathbf{P}(\mathbf{x}, t) - \kappa(\mathbf{x}, t) = 0$
quasi static approximation, inertial term are neglected (time duration of the "heat pulse" \gg time propagation of a elastic wave)
volume forces (gravity) neglected in comparison to thermal stress
BC: symmetry plane: $\mathbf{n} \cdot \mathbf{u} = 0$, bottom edge, $u_z = 0$; back face $u_y = 0$

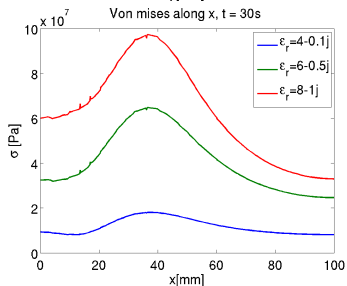
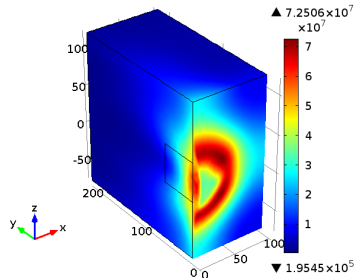
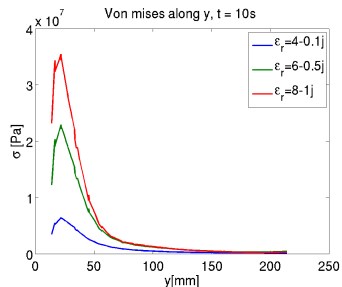
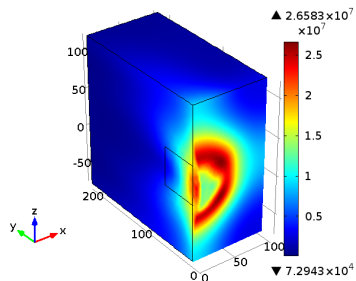
RESULTS, E FIELDS, POWER DENSITY



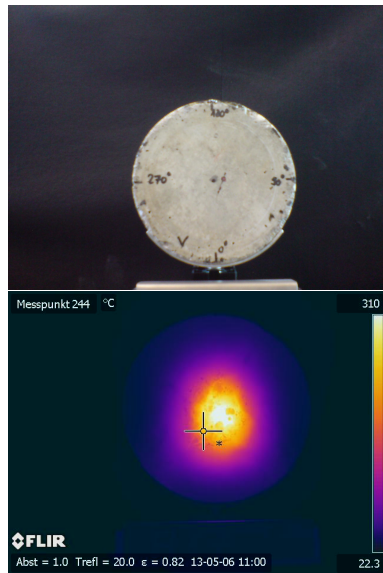
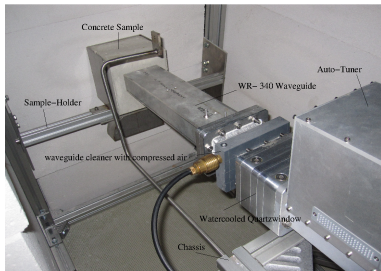
TEMPERATURE ($^{\circ}\text{C}$) AND THERMAL GRADIENT FIELDS



STRESS FIELDS $t = 10, 30$ s



TEMPERATURE MEASUREMENTS



Conclusion

- A thermo elastic model of microwave heating of concrete is useful for the design of an applicator
- It allows to calculate the electric field, power density, displacements and stress fields
- pore pressure and water movements are not taken into account with the current model
- Experimental tests shows that ablation size is function of the input power, water content, porosity and sample size

Further work

- antenna matching
- higher frequency
- mechanics: optimal stress pattern?
- modelling: porous model with water and vapour transport
- temperature and displacements measurements

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Thank you for your attention