

# Simulation of rarefied gasflow in the KATRIN tritium source

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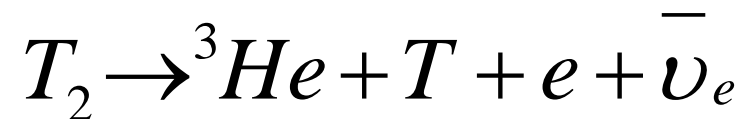



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# 1. THE KATRIN EXPERIMENT - A (SHORT) INTRODUCTION

- „Who“ is KATRIN? – Karlsruhe Tritium Neutrino Experiment
- Measurement of absolute neutrino mass through beta decay of  $T_2$



- Measurement of electron spectrum with MAC-E Filter  
(*Magnetic adiabatic Collimation with Electrostatic Filter*)
- Limit Today:  $m_\nu < 3\text{eV}$  → possible KATRIN limit:  $m_\nu < 200\text{meV}$
- Higher sensitivity through :  
larger experiment, higher luminosity, lower background,  

**reduction of systematic errors** (Gasdynamics...)  
**precision of simulated integrated density <0.2%!!!!**

# 1.1 Tritium Source WGTS (*Windowless Gaseous Tritium Source*)



*Fig: 1.1.1 Planned WGTS design*

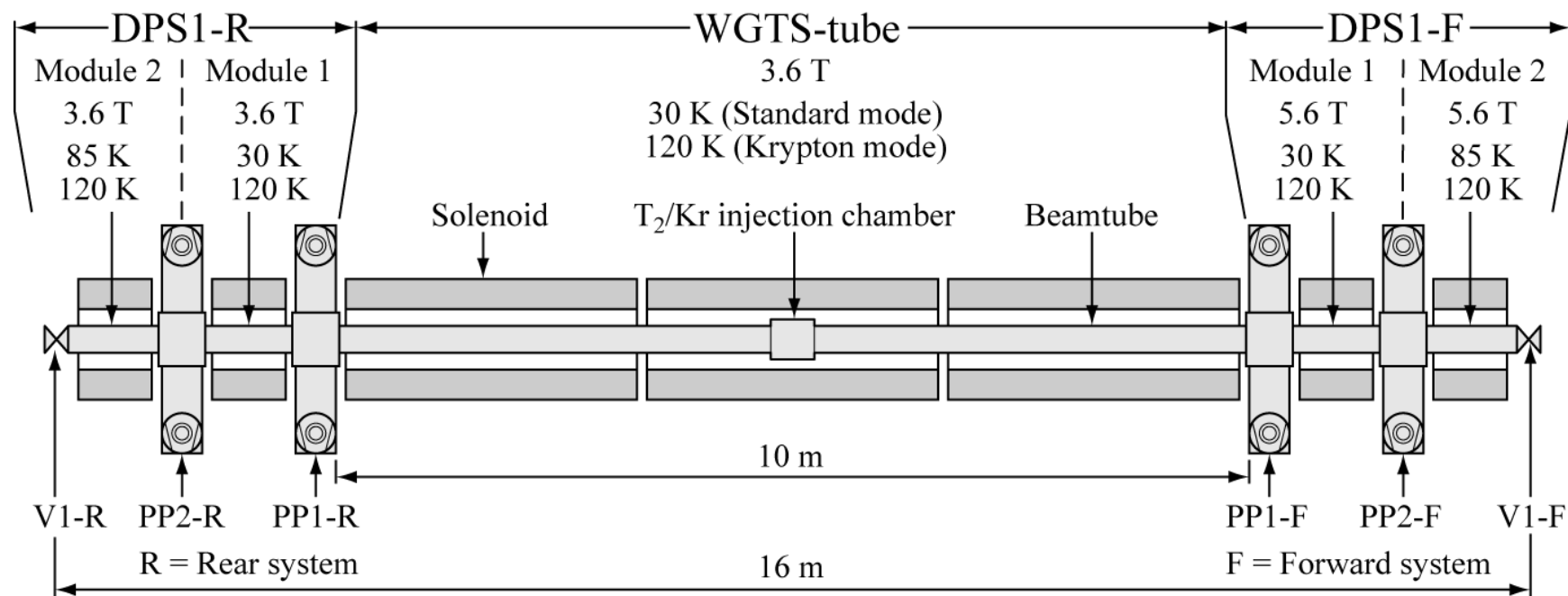


Fig. 1.1.2 WGTS scheme

- 10 m stainless steel tube, diameter 90mm
- High Temperature stability at 27-30K
- T<sub>2</sub> injection with pressure of 0.336 Pa through small orifices
- Avoid Tritium in spectrometer → 10<sup>14</sup> pressure reduction factor
- Reduction factor WGTS end: 10<sup>3</sup>

# **2. KATRIN GASDYNAMIC SIMULATION – A STATUS REPORT**

## 2.1 General description of flow regimes in the WGTS

$$\delta = \frac{R \cdot p(z)}{\mu v_m}$$

$\delta$  = Rarefaction parameter

- **At Injection:**  
 $p \approx 0.335 \text{ Pa} \rightarrow \delta \approx 23.4$  Continuum, Navier Stokes equations
- **After 1<sup>st</sup> pump:**  
 $p \approx 0.003 \text{ Pa} \rightarrow \delta \approx 0.2$  Free molecular, collisions neglectable
- **In tube and 1<sup>st</sup> pump port:**  
 $0.02 < \delta < 23$  Collision term not neglectable (transition region), Boltzmann equation



## 2.2 Gasflow simulations of Felix Sharipov

- Numerical calculations based on Boltzmann equation (BE)
- Assumes BGK equation with S-model modification
- Gas – surface interaction included by Cercignani–Lampis scattering kernel
- Geometry and assumptions systematically improved:
  - Exit pressure  $\neq 0$
  - Inlet and end effects
  - Longitudinal and radial temperature variation
  - 2D calculations (with temperature gradient)
  - To be continued with calculation of gas flow in first pump port...

- $R/l = 0.0045 \rightarrow$  first 1D calculation with  $p_{ex} = 0, T = \text{const.}$

- Reduced flow rate  $G$  and local reduced flow rate  $G_p$  connected:

$$G = \frac{v_m (L/2)}{\pi R^3 p_{in}} \dot{M}$$

$$G_p = -\frac{v_m}{\pi R^3} \cdot \frac{dz}{dp} \cdot \dot{M}$$



$$G_p \frac{(L/2)}{\delta_{in}} \cdot \frac{d\delta}{dz} = -G$$

- $G_p(\delta)$ 's from kinetic BE, calculate  $\delta$ -values numerically
- Interpolation formula for  $\delta(z)$  for KATRIN source simulation
- Next steps:
  - T-profile and  $p_{ex} \neq 0$  considered
  - Inlet and end effects considered

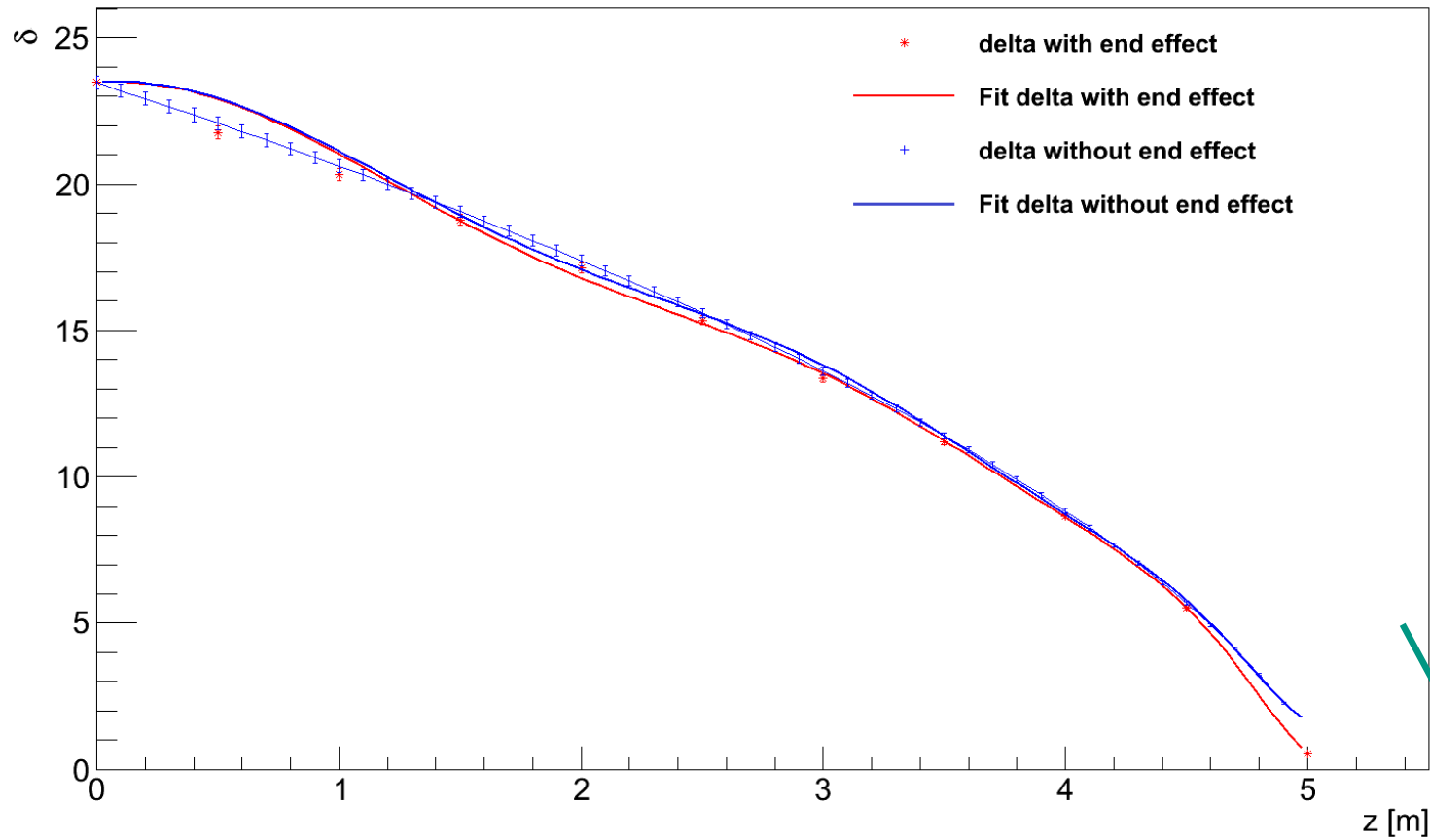
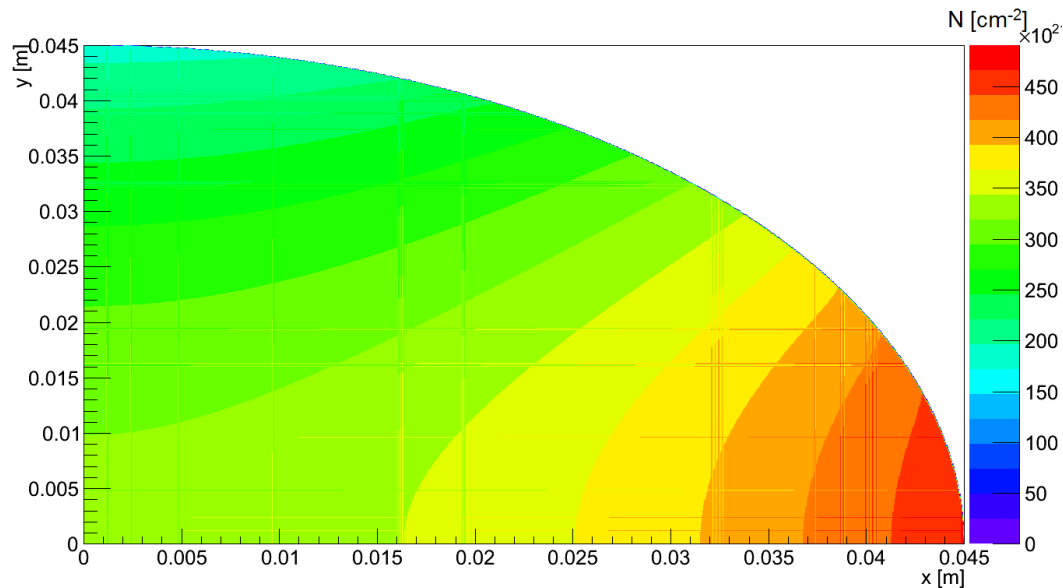


Fig.2.2.1 Rarefaction parameter  $\delta$  with and without end effect ( $p_{ex}=5\%p_{in}$ )

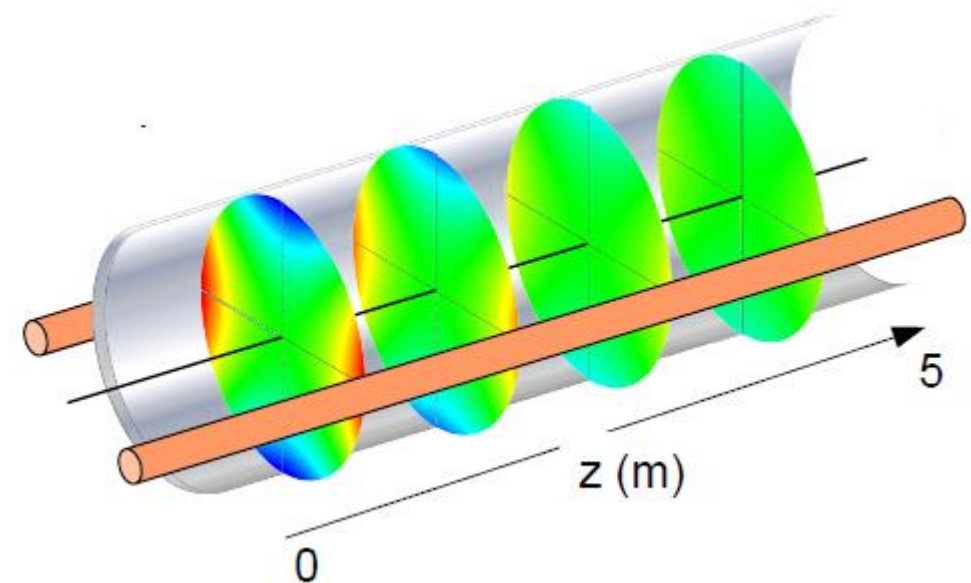
Error from not considering end effects:  $z < 4\text{m}$ ,  $\Delta < 2.5\%$   
 $z = 4.5\text{m}$ ,  $\Delta \approx 4.5\%$

## 3D calculation :

- Same approach for solving BE as in 1D calculations
- Large computational effort → pseudo 3D-profil:  
2D calculations (include  $\Delta T$  but no end effects) for 25  $\delta$ -values
- Combine with  $\delta(z)$  from 1D calculation → 3D profile



*Fig 2.2.2 2D density profile at  $z=0$*

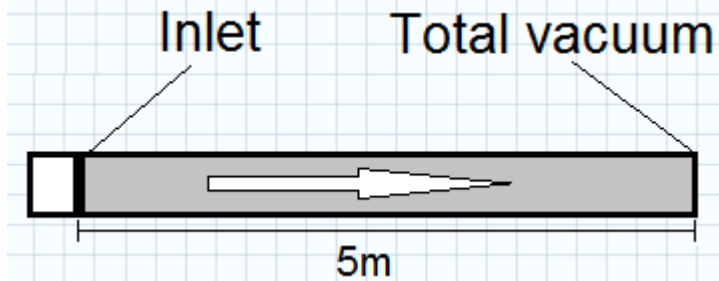


*Fig 2.2.3 Pseudo 3D profile*

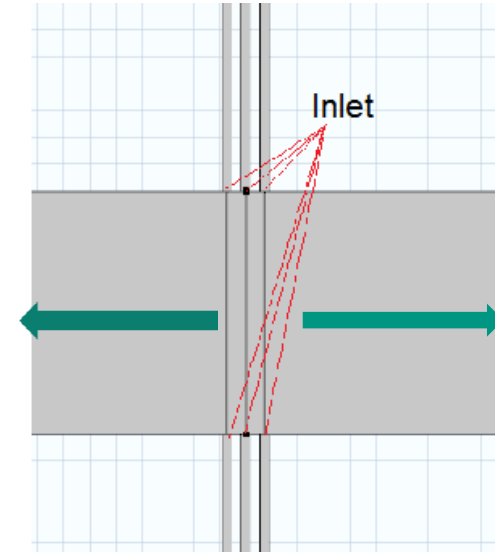
# 3. THE WGTS IN COMSOL

# 3.1 2D Geometry

1. Simplified tube for comparison with 1<sup>st</sup> Sharipov data:

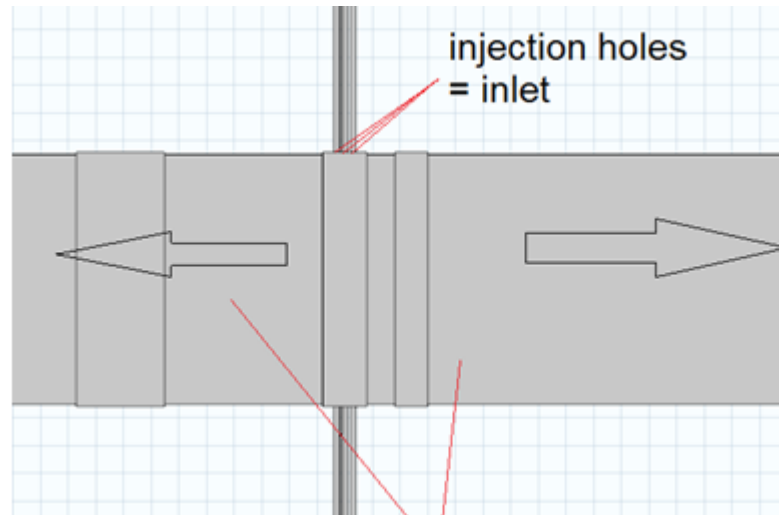


2. As 1. with exact inlet configuration:

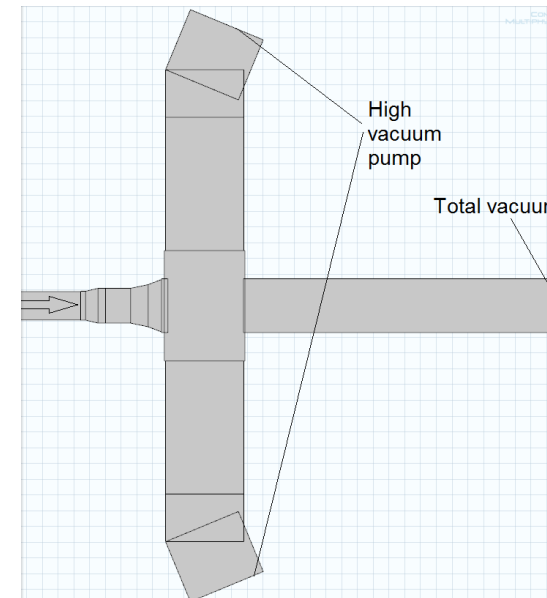


3. Exact WGTS geometry:

Inlet region:



Outlet region:

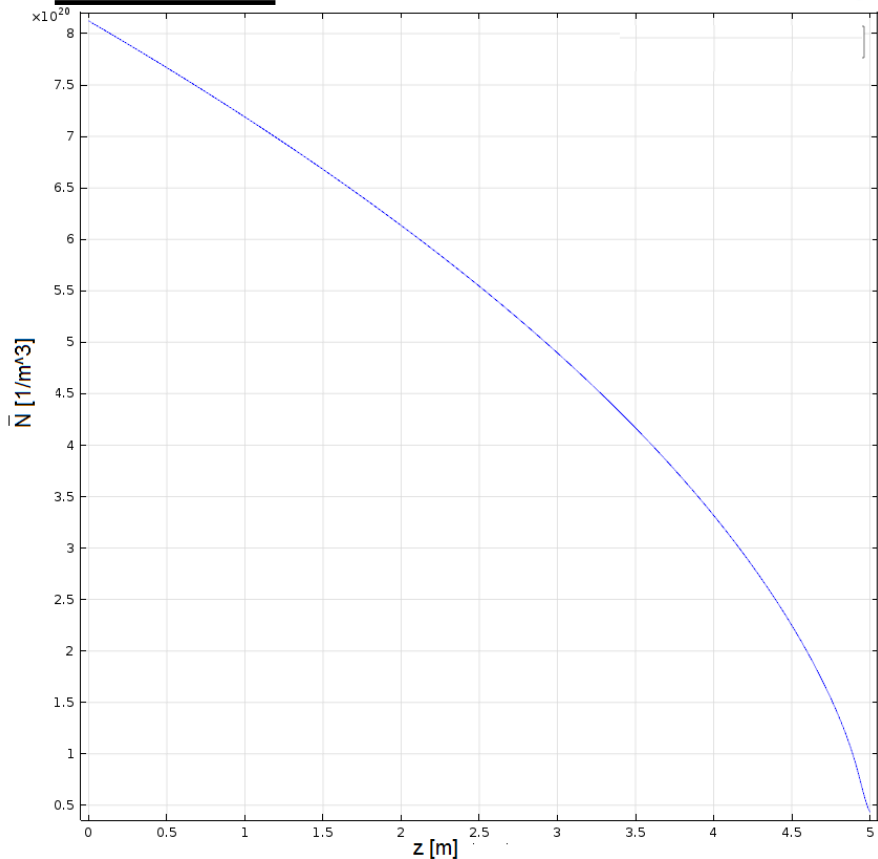


# Transitional Flow Parameter:

$P_{in} = 0.3368 \text{ Pa}$ ,  $M = 6.003 \text{ kg/mol}$

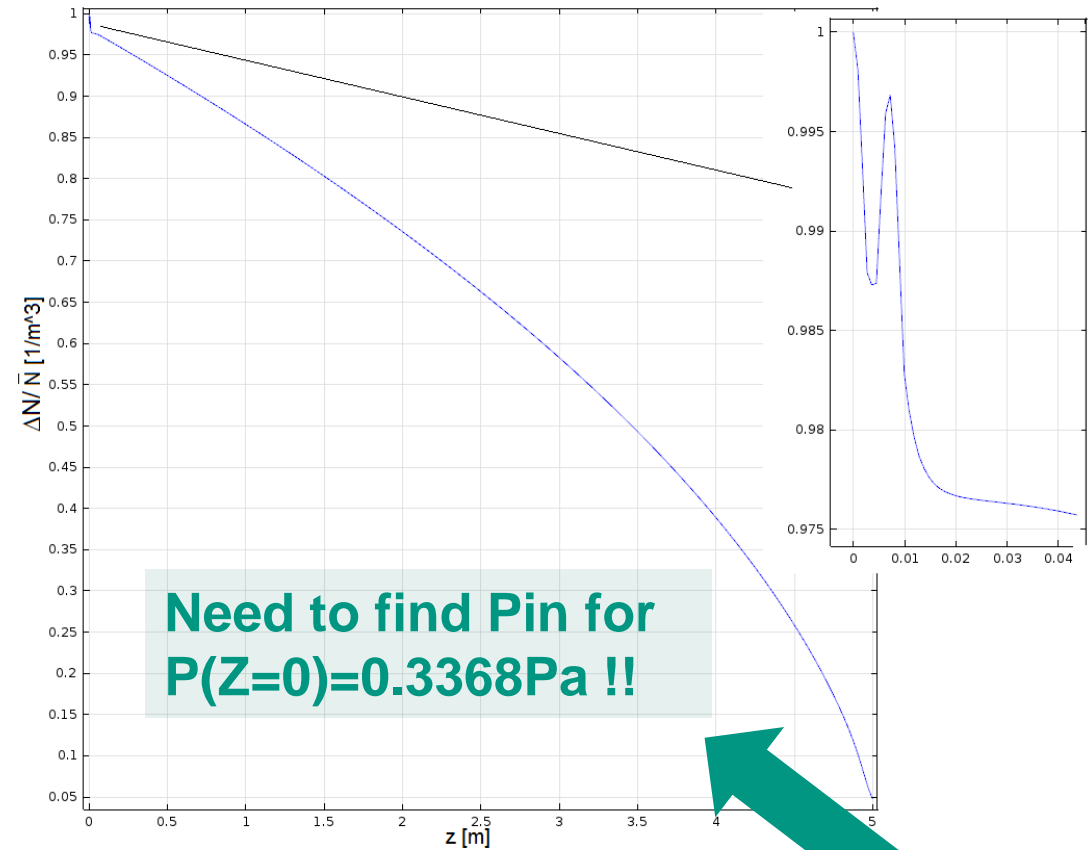
$T = 30\text{K} = \text{const !!!}$ ,  $\mu = 2.245 \cdot 10^{-6} \text{ Pa}\cdot\text{s}$

## Case 1:

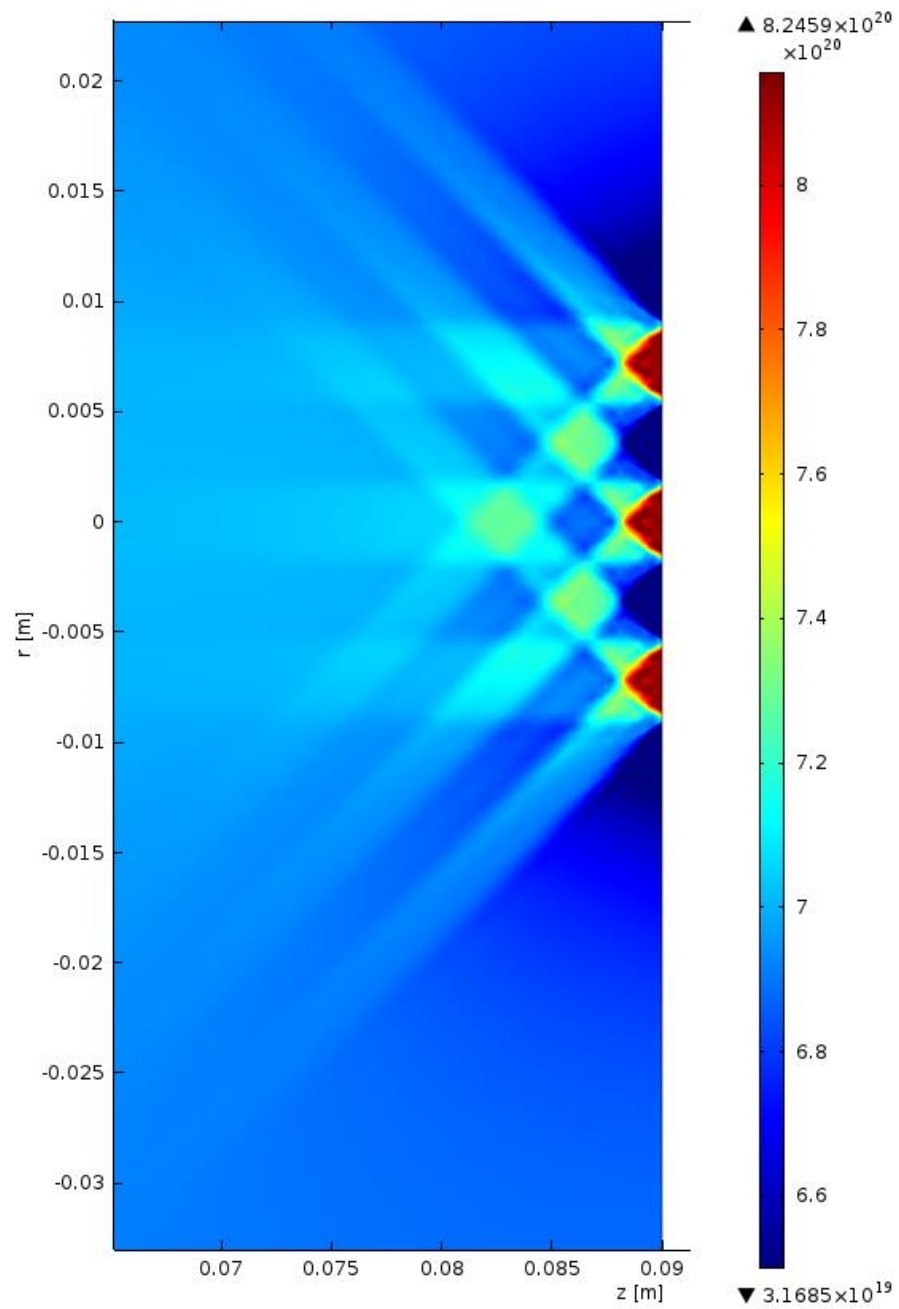


*Fig. 3.1. Average  $N(z)$ ,  
 $N_{\text{average tube end}} = 5.3\% N_{in}$ ,  
 $N_{\text{col}} = 5.12 \cdot 10^{21} \text{ m}^{-2}$*

## Case 2:



*Fig. 3.2. Average  $N(z)$   
 $N_{\text{average at tube end}} = 4.7\% N_{in}$ ,  
 $N_{\text{col}} = 4.4 \cdot 10^{21} \text{ m}^{-2}$ ,  $P_{\text{average}}(z=0) = 0.292 \text{ Pa}$*



*Fig. 3.1. Number density in injection region*



# 4. Sharipov vs. COMSOL simulation

# a) Comparison COMSOL vs Sharipov data without end effect

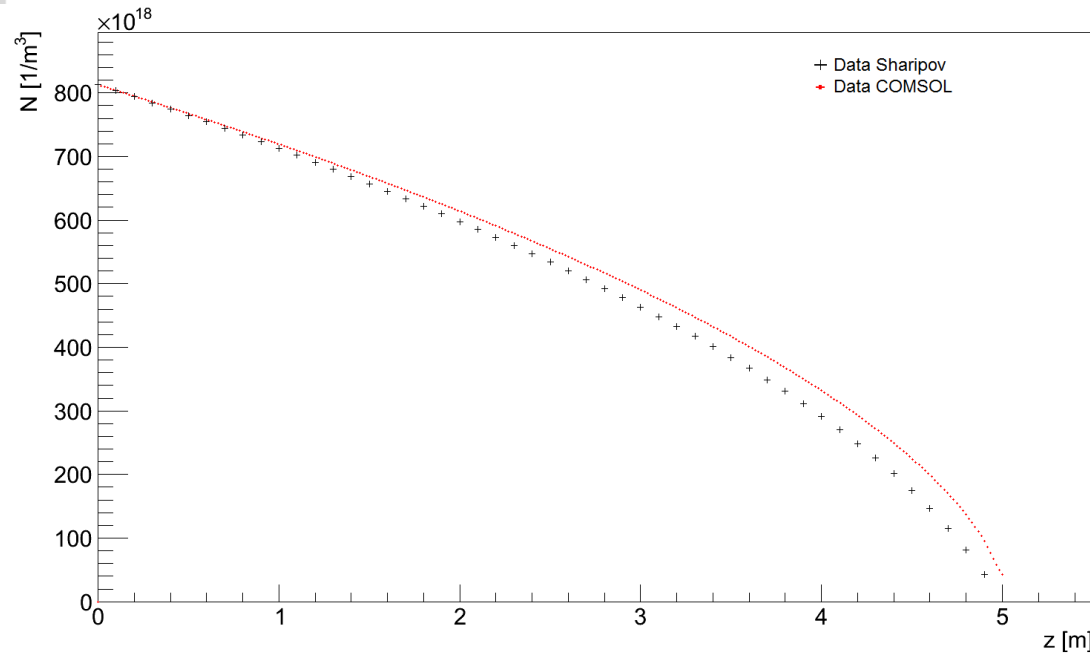


Fig. 4.1  $N(z)$  simple inlet configuration and Sharipov simulation with  $p_{ex}=0.53p_{in}$

Deviation in column density 2.5%

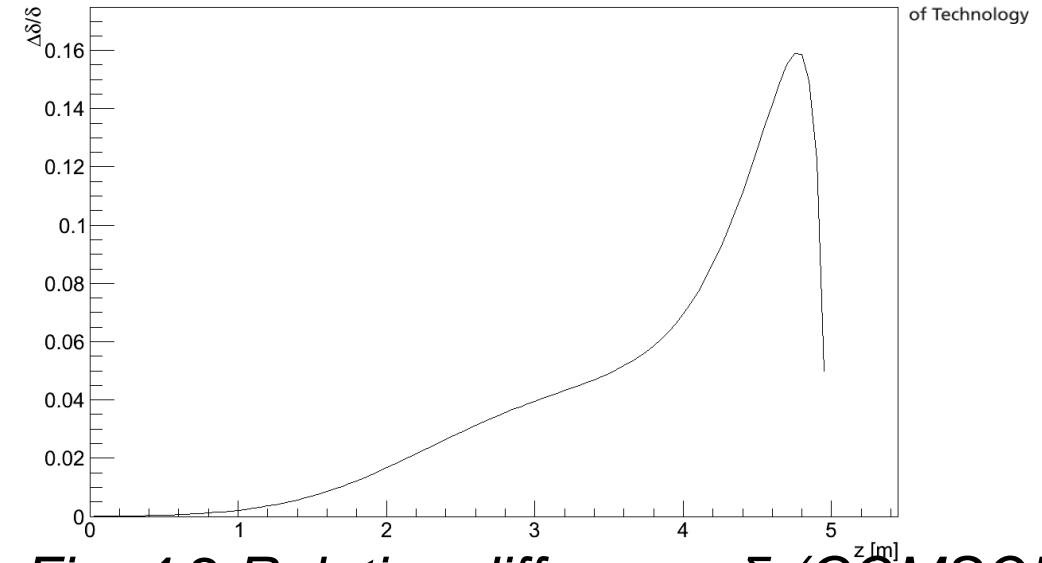


Fig. 4.2 Relative difference  $\delta$  (COMSOL vs Sharipov)

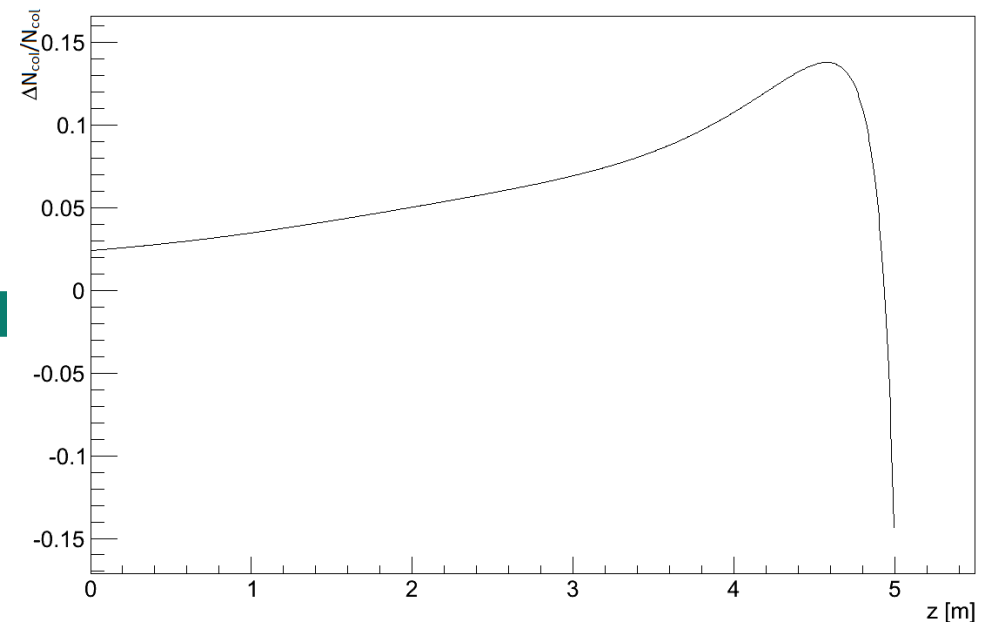
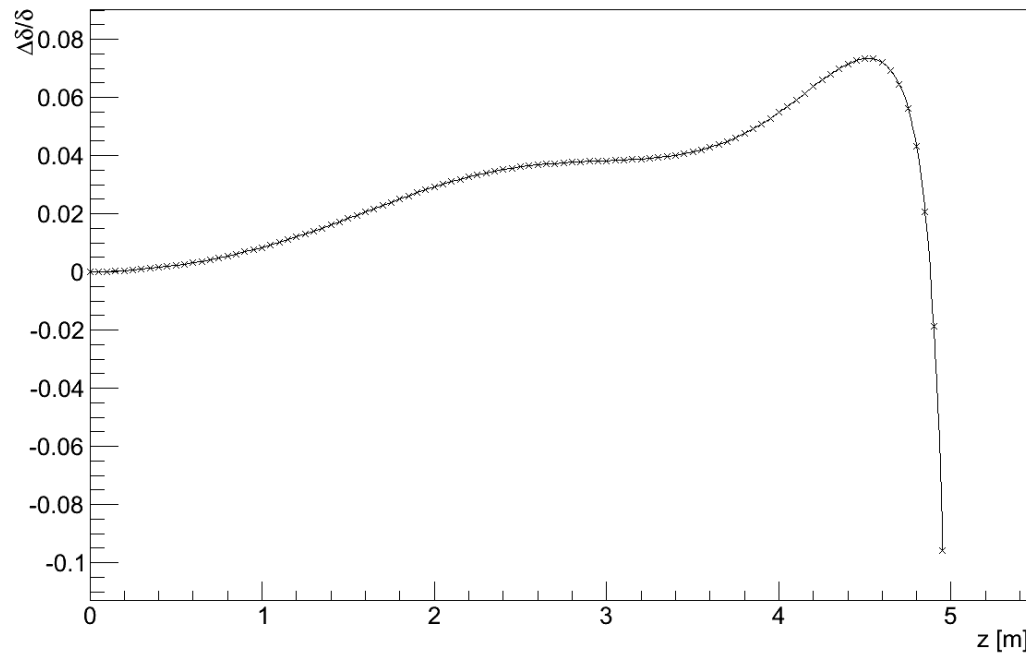


Fig. 4.3 Relative difference  $N_{col}$

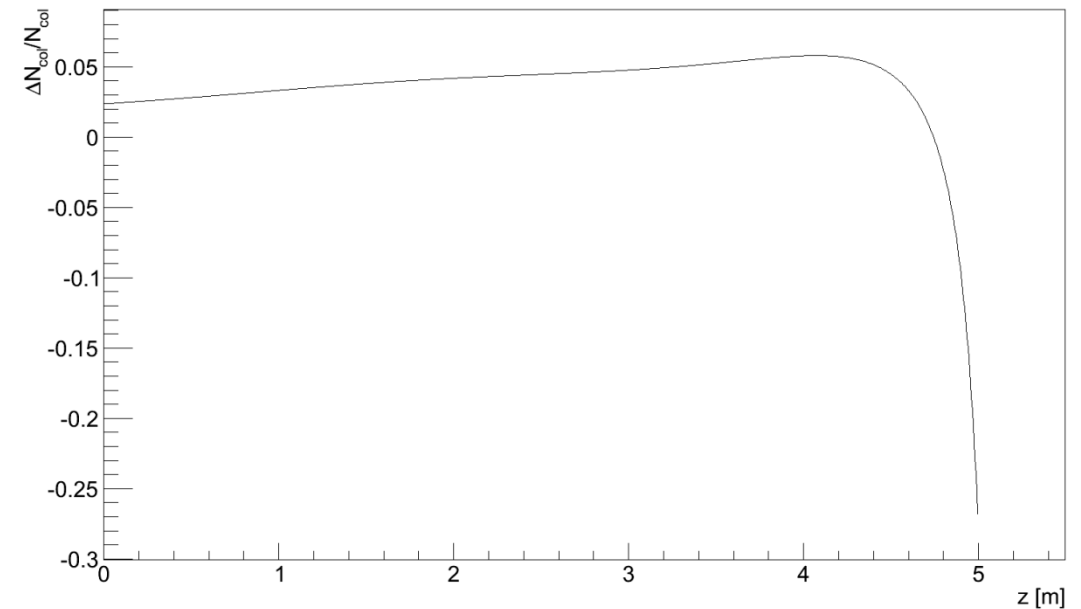
## b) Comparison COMSOL vs Sharipov data with end effect



*Fig. 4.4 Relative difference  $\delta$  (3 fold inlet configuration)*



Still 2.5% deviation in column density



*Fig. 4.5 Relative difference  $N_{col}$*

# 5. CONCLUSION

- Different 2D models of the WGTS using Transitional flow interface had been simulated with COMSOL
- Comparison of average 2D results with 1D Sharipov calculation:
  - Deviations in density of end region (up to 8%)
  - Disagreement in column density (for  $z=0$ ) 2.5%, KATRIN needs  $N_{col}$  precision of 0.2%...
  - Disagreement in pressure distribution inlet region
- No  $\Delta T$  and accommodation coefficient in COMSOL simulation
- **ToDo:** improve 2D simulation (all pump ports, mesh size), simulate 3D geometry, find correct inlet pressure, simulate test experiment

Thank you for  
your  
attention...