



# Residual stress in Silicon membranes of circular CMUT

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CONFERENCE  
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# Outline



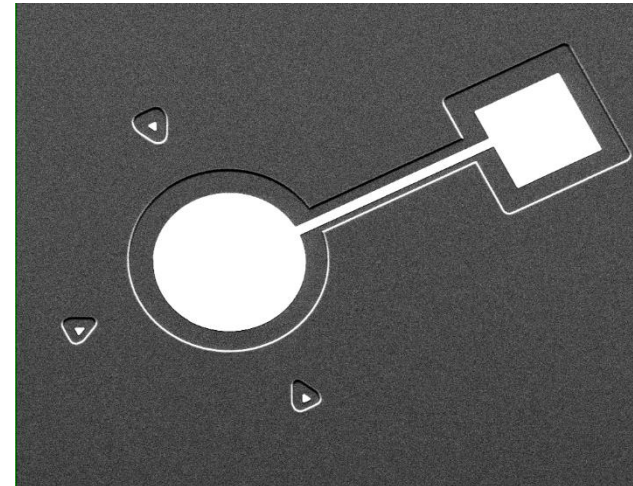
## ❖ Introduction

- Key parameters
- Fabrication of CMUT
- Experimental results

## ❖ Comsol model

## ❖ Results

## ❖ Conclusions



**SEM image of cavity and bottom electrode of a single CMUT**

# Introduction

## What is CMUT?

Capacitive Micromachined Ultrasound Transducer

Energy converters from electrical to mechanical domain and vice versa

## Why CMUT?

Wide bandwidth

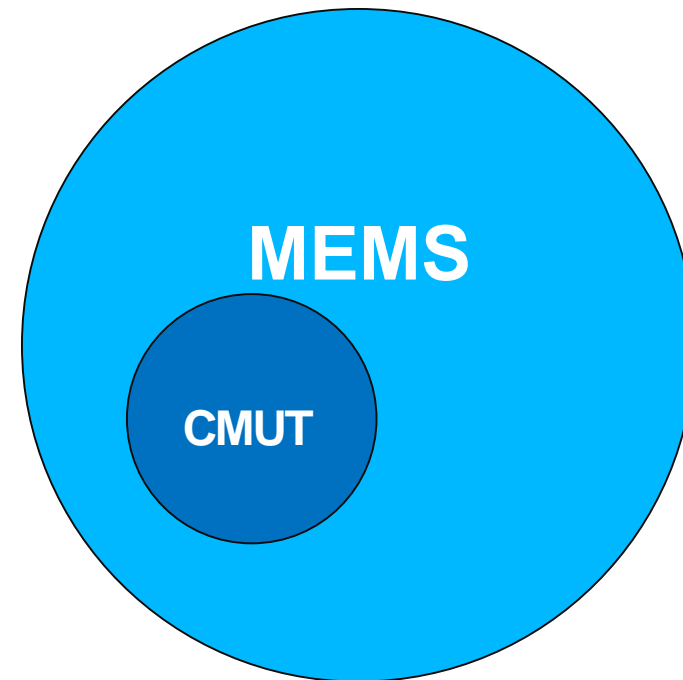
Compatibility with standard CMOS processes

## Application

Ultrasound Imaging System (liquid, tissue)

Flow sensors (air)

Structural Health Monitoring (solid)



# Key parameters

## Electrostatic force

$$F_E = \frac{1}{2} \frac{C(x)}{d_{eff}-x} V^2, \quad C(x) = \frac{\epsilon \epsilon_0 S}{d_{eff}-x}, \quad V = V_{DC} + V_{AC};$$

**Electrostatic softening effect:** elastic restoring force

$$k = k_m + k_e = k_m - \frac{C(x)}{(d_{eff}-x)^2} V^2$$

## Pull-In Voltage

$$V_{PI}: k_m + k_e = 0$$

## Electromechanical coupling

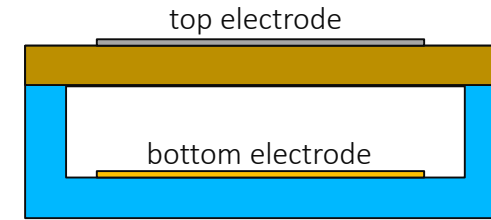
$$k_T^2 = \frac{2x}{d_{eff}-x + (d_{eff}-3x) \frac{C_p}{C(x)}}$$

## Eigenfrequency

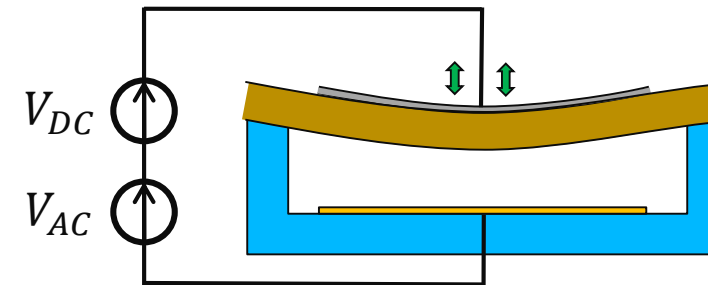
$$f_0 = \frac{1}{2\pi} \sqrt{\frac{k_m + k_e}{m}}$$

## Bandwidth

$$\frac{\Delta f}{f_0} = \frac{f_2 - f_1}{f_0}$$



Schematic cross-section of CMUT structure



# Fabrication of CMUT

## Fabrication approach:

- **Sacrificial release process**
- **Wafer bonding technique**

Radius of CMUT R: **50, 70, 100, 150**  $\mu\text{m}$

Radius of the bottom electrode: **0,8\*R**

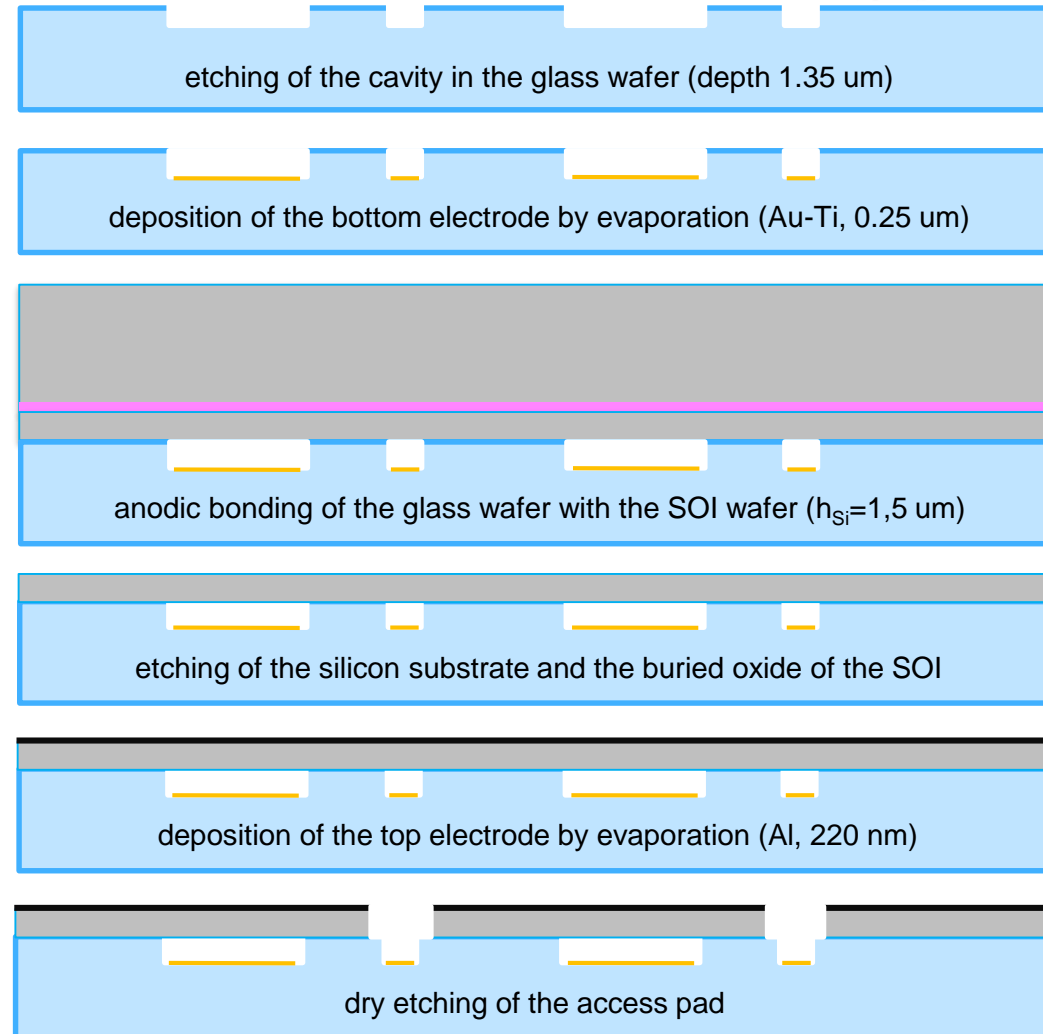
Gap: **1,1**  $\mu\text{m}$

Thickness of Silicon, (100) plane : **1,5**  $\mu\text{m}$ ;

Thickness of Al: **0,22**  $\mu\text{m}$ ;

Residual stress appears due to fabrication steps process:

- SOI wafer with prestressed Si layer;
- anodic wafer bonding;
- Al deposition.

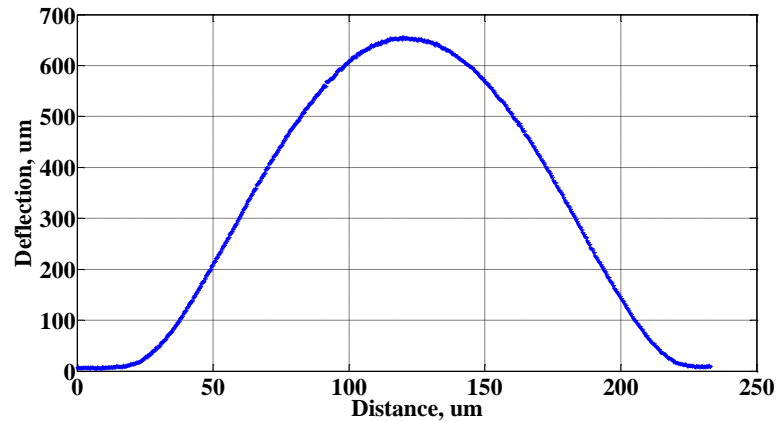


# Experimental results



Radius, $\mu\text{m}$	Maximum static deflection, nm	Eigenfrequency, MHz (FEM)	Eigenfrequency*, MHz (exp.)
50	142	2,28	2,3
70	360	1,18	1,26
100	650	0,58	0,82
150	1500	0,26	0,6

\*in air



Typical static deflection after fabrication (R=100  $\mu\text{m}$ )

## Static deflection

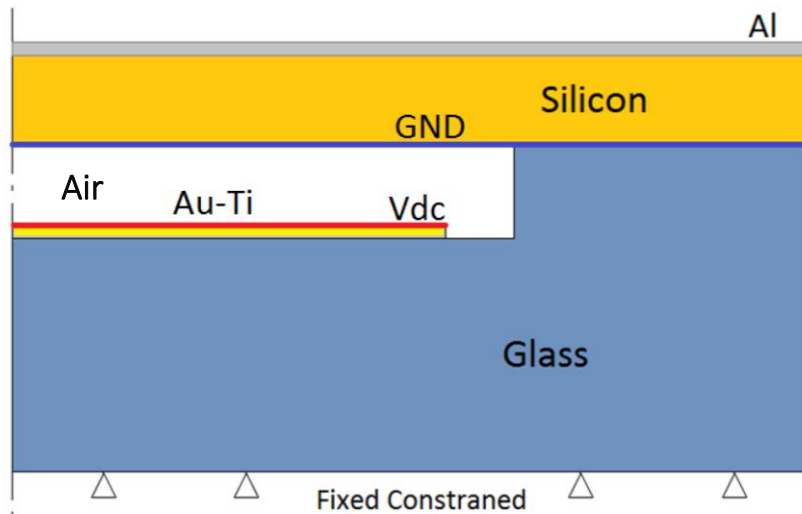
residual stress

## Eigenfrequency

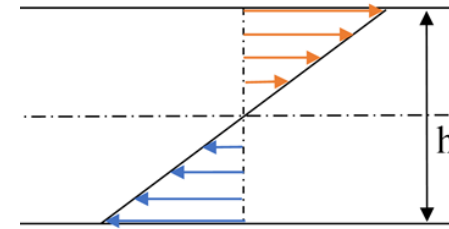
residual stress

air spring effect

# Comsol model



Cross sectional view of CMUT cell with applied mechanical and electrical boundary conditions



Bending stress distribution in Silicon

$$S_r = S_0 \frac{z}{(h/2)}$$

Types of studies:

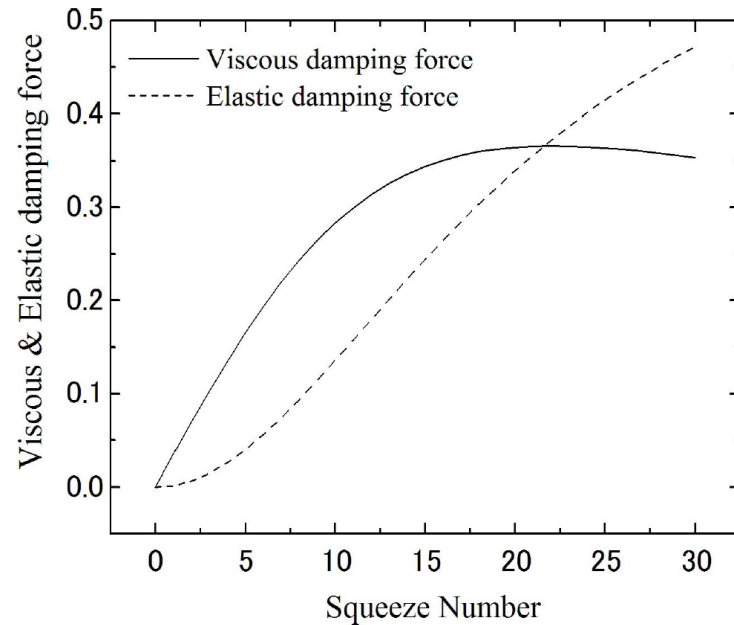
- Stationary study (deflection, pull-in voltage)
- The Prestressed Analysis, Eigenfrequency study (deflection, eigenfrequency)
- The Prestressed Analysis, Frequency Domain (deflection, bandwidth, coupling)

# Air spring effect

$$m\ddot{y} + c_d\dot{y} + (k_0 + k_e)y = F_0 \sin(\omega t)$$

$k_e$  - the coefficient of viscous damping force,

$c_d$  - the coefficient of elastic damping force



Dependences of the viscous and the elastic damping forces of CMUTs on the squeeze number. The membrane plate is assumed to be a square.\*

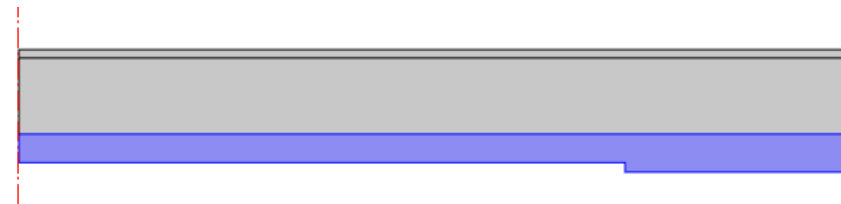
$$\sigma = \frac{12\mu\omega R^2}{P_a h_0^2} - \text{squeeze number}$$

$$\sigma = 36,2$$

$$\sigma \gg \sigma_c: \quad k_e = \frac{P_a A}{h_0}, \quad c_d \cong 0$$

$$\omega_0 = \sqrt{\frac{k_0}{m}} \rightarrow \omega_e = \sqrt{\frac{k_0 + k_e}{m}} - \text{air spring effect}$$

## FEM model



Grey area - Solid Mechanics

Blue area - Pressure Acoustics,

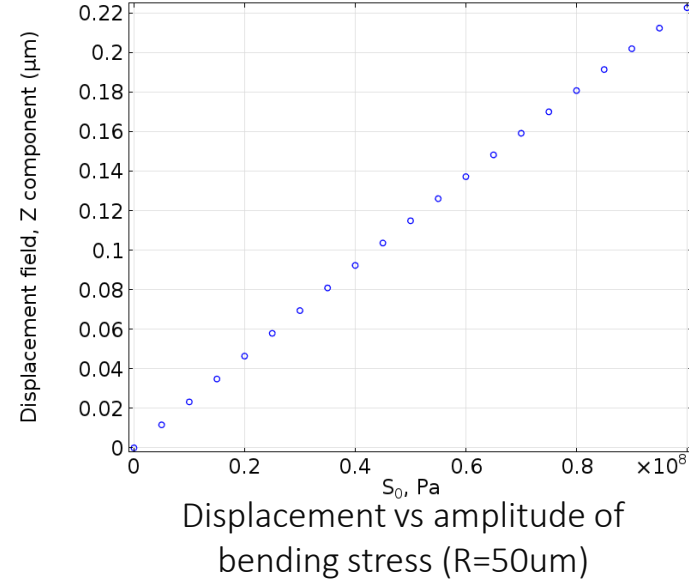
Linear elastic fluid model ( $k_e = \frac{P_a A}{h_0}$ ,  $c_d = 0$ )

\*Lee, S. M., Cha, B. S., & Okuyama, M. (2011). Viscous Damping Effect on the CMUT Device in Air. JOURNAL OF THE KOREAN PHYSICAL SOCIETY, 58(4), 747-755.



# Residual stress calculation

Radius, $\mu\text{m}$	Maximal static deflection, nm
50	142
70	360
100	650
150	1500

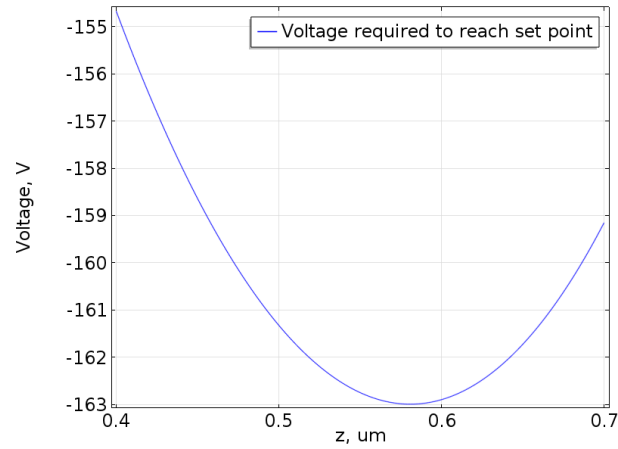


R, $\mu\text{m}$	$S_0$ , MPa (defl)	Eigenfrequency, MHz (FEM)	Eigenfrequency <sup>1</sup> , MHz (FEM)	Eigenfrequency, MHz (exp.)
50	63,5	2,28	2,31	2,3
70	86,0	1,18	1,29	1,26
100	76,5	0,58	0,88	0,82
150	78,7	0,26	0,65	0,6

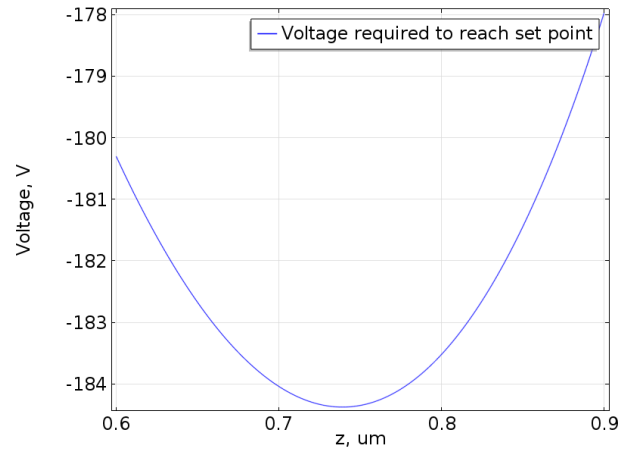
<sup>1</sup> with considering air spring effect and geometric nonlinearity

# Results

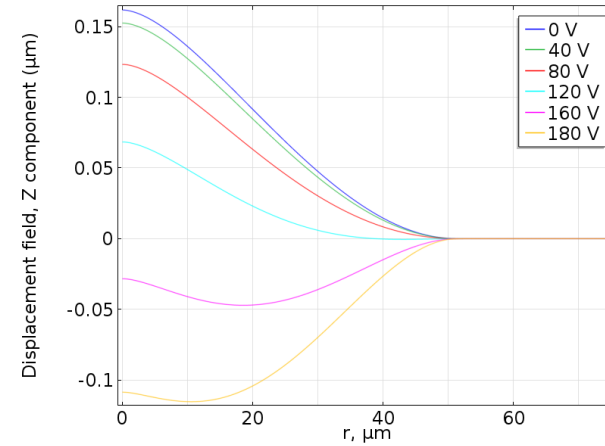
Pull In Voltage calculation



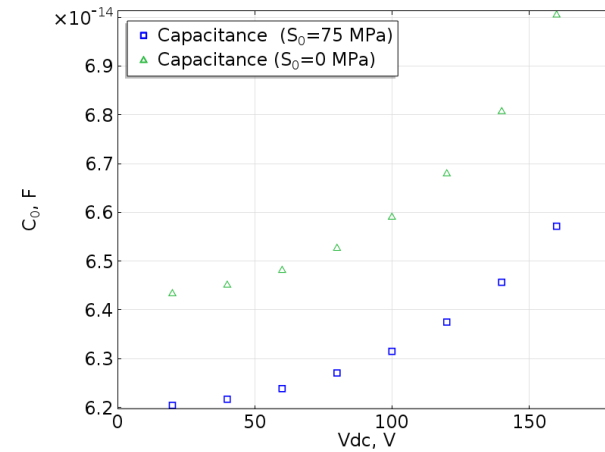
$V_{PI}=163 \text{ V}$  ( $S_0=0 \text{ MPa}$ ,  $R=50\mu\text{m}$ )



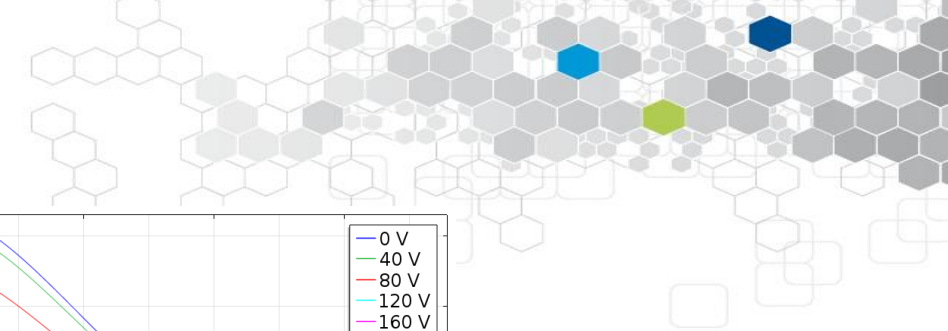
$V_{PI}=184,4\text{V}$  ( $S_0=75 \text{ MPa}$ ,  $R=50\mu\text{m}$ )  
exp.  $V_{PI}=180 \text{ V}$ ,  $\sigma=19,8 \text{ V}$



Vertical displacement of CMUT membrane for different dc bias voltage ( $S_0=75\text{MPa}$ ,  $R=50\mu\text{m}$ )



Capacitance vs dc bias voltage with and without stress ( $R=50\mu\text{m}$ )



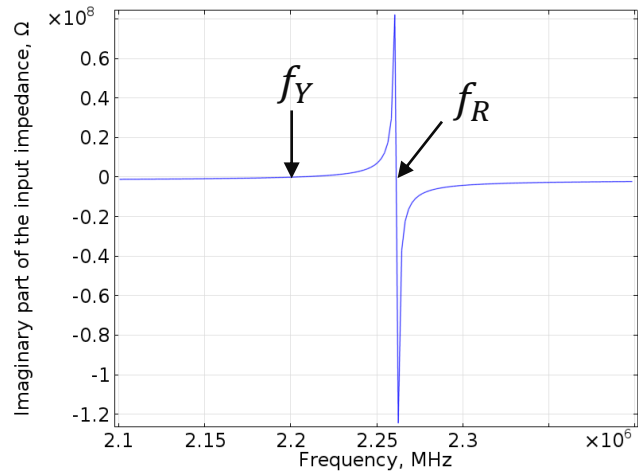
# Results

Coupling factor

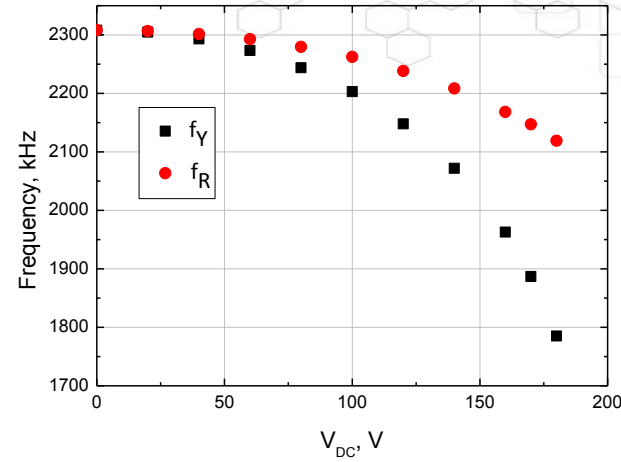
$$k_T^2 = 1 - \left( \frac{f_Y}{f_R} \right)^2$$

$f_Y$  - resonance frequency

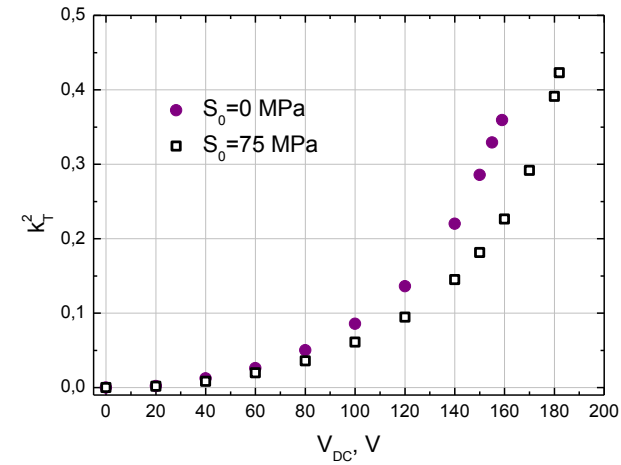
$f_R$  - antiresonance frequency



Imaginary part of the input impedance of the CMUT  
( $V_{DC}=100$  V,  $S_0=75$ MPa,  $R=50$ um)



Resonance and antiresonance frequencies vs biased voltage  
( $S_0=75$ MPa,  $R=50$ um)



Coupling factor vs dc bias voltage  
with and without stress

# Conclusions



- We used COMSOL Multiphysics MEMS module to obtain the value of bending stress with parametric sweep. The average value of amplitude of bending stress is 75 MPa
- COMSOL provides better understanding of static and dynamic behavior of CMUT (air spring effect, pull in voltage, capacitance, coupling)
- The calculated results are in a good agreement with experimental data

## Future plans and final goal

- Test of CMUTs in vacuum chamber
- Developing approach for application of CMUT in structural health monitoring



# Thank you!



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