## Sound Pressure Amplification using-FP Resonance of Acoustic Metamaterial Cavity

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1. Physical Property Augmentation using Metamaterials
2. Coiled-up Space Acoustic Metamaterial Amplification Cavity
3. Applications


## EM Property Augmentation using Metamaterials

- Metamaterials are periodic or quasi-periodic, sub-wavelength metal structures. The material properties are derived from its structure rather than inheriting them directly from its material composition.

empty glass $\mathbf{n}=1$

regular water, $\mathrm{n}=1.3$

"negative" water, $\mathrm{n}=-1.3$


## EM Property Augmentation using Metamaterials



- In electromagnetics, electric permittivity( $\varepsilon$ ), and magnetic permeability $(\mu)$ are the two fundamental parameters characterizing the EM property of a medium.
- Depending on the signs of $\varepsilon$ and $\mu$, materials can be categorized into 4 groups.


## EM Property Augmentation using Metamaterials

SOVIET PHYSICS USPEKHI
VOLUME 10, NUMBER 4
JANUARY-FEBRUARY 1968
538.30

THE ELECTRODYNAMICS OF SUBSTANCES WITH SIMULTANEOUSLY NEGATIVE $V A L U E S$ OF $\in A N D \mu$
V. G. VESELAGO
P. N. Lebedev Physics Institute, Academy of Sciences, U.S.S.R.

Usp. Fiz. Nauk 92, 517-526 (July, 1964)

1. INTRODUCTION
$T_{\text {HE dielectric constant } \epsilon \text { and the magnetic permea- }}$
II. THE PROPAGATION OF WAVES IN A SUBSTANCE WITH $\epsilon<0$ AND $\mu<0$. "RIGHT-HANDED" AND "LEFT-HANDED" SUBSTANCES

- The first theoretical study was performed by V.G. VESELAGO and it took nearly 30 years for experimental verification.


## EM Property Augmentation using Metamaterials

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Composite Medium with Simultaneously Negative Permeability and Permittivity
D. R. Smith,* Willie J. Padilla, D. C. Vier, S. C. Nemat-Nasser, and S. Schultz
Department of Physics, University of California, San Diego, 9500 Gilman Drive, La Jolla, California 92093-0319
(Received 2 December 1999)
```

- D.R. Smith showed simultaneous negative permeability and permittivity for the first time.

VOLUME 85, NUMBER 18
PHYSICAL REVIEW LETTERS
30 OCTOBER 2000

Negative Refraction Makes a Perfect Lens
J. B. Pendry

Condensed Matter Theory Group, The Blackett Laboratory, Imperial College, London SW7 2BZ, United Kingdom (Received 25 April 2000)

- J.B. Pendry proposed concept of perfect lens using negative refractive index and this is the most famous work in the world of metamaterials.


## EM Property Augmentation using Metamaterials



Split Ring Resonator (SRR)
$\varepsilon(\omega)=\varepsilon_{o}\left[1-\frac{\omega_{p}^{2}}{\omega(\omega+i \gamma)}\right]$
$\omega_{p}=N e^{2} / m \varepsilon_{o}$ is the plasma frequency in which the collection of electrons oscillate in the presence of electric field. When $\gamma=0$ and $\omega<\omega_{\mathrm{p}}$ negative permittivity is achieved. For most materials, when $\omega<\omega_{\mathrm{p}}$, $\omega \ll \gamma$ (absorption dominated). Using subwavelength periodic rods, it is possible to increase the effective mass of the electrons which decrease the $\omega_{p}$. SRRs create RLC circuit.

## EM Property Augmentation using Metamaterials

Negative refraction: $\varepsilon<0, \mu<0$


- SRR and solid rod composite material was used to achieve double negative material.
- Periodic unit cells act as 'meta-atoms' which show effective medium properties in subwavelength regime.


## EM Property Augmentation using Metamaterials



- Many extraordinary properties are being discovered and new systems such as super lens, cloaking, reverse Doppler etc are being researched.
- However very narrow resonance bandwidth and high losses are problems for EM metamaterial systems.


## Analogy between Acoustics and EM

| Acoustics | Electromagnetism (THz) | Analogy |
| :---: | :---: | :---: |
| $\frac{\partial P}{\partial x}=-i \omega \rho_{x} u_{x}$ | $\frac{\partial E_{z}}{\partial x}=-i \omega \mu_{y} H_{y}$ |  |
| $\frac{\partial P}{\partial y}=-i \omega \rho_{y} u_{y}$ | $\frac{\partial E_{z}}{\partial y}=i \omega \mu_{x} H_{x}$ |  |
| $\frac{\partial u_{x}}{\partial x}+\frac{\partial u_{x}}{\partial y}=-i \omega \beta P$ | $\frac{\partial H_{y}}{\partial x}-\frac{\partial H_{x}}{\partial y}=-i \omega \epsilon_{z} E_{z}$ |  |
| Acoustic pressure $P$ | Electric field $E_{z}$ |  |
| Particle velocity $u_{x} u_{y}$ | Magnetic field $H_{x} H_{y}$ | $H_{y} \leftrightarrow-U_{x} H_{x} \leftrightarrow u_{y}$ |
| Dynamic density $\rho_{x} \rho_{y}$ | Permeability $\mu_{x} \mu_{y}$ | $\rho_{x} \leftrightarrow \mu_{y} \rho_{y} \leftrightarrow \mu_{x}$ |
| Dynamic compressibility $\beta$ | Permittivity $\varepsilon_{z}$ | $\varepsilon_{z} \leftrightarrow \beta$ |

- 1 to 1 correspondence is possible between acoustics and Electromagnetism.
- Therefore many EM metamaterial related phenomenon can be replicated in the acoustic regime and more.


## Coiled-up Space Metamaterial Design



Unit Cell
( 1 cm )


Acoustic Wave
Propagation

- Solid structure which results in a 'zigzag' path is designed.
- Acoustic waves must travel along this zigzag path rather than the straight path.
- The subwavelength structure create an effective medium.


## Double-fish net Metamaterial Cavity

Single-walled Metamaterial Slab


Double-walled Metamaterial Slab


- FP like resonance modes are present for the single-walled metamaterial slab.
- FP is modified and strong amplification phenomena exists inside the cavity


## Reduced Reflection Coefficient




Metamaterial
Slab 1 Slab 2
Aluminum Duct



- First experimental results show sharp drop in the reflection coefficient at the fundamental FP resonance frequency


## Emission Enhancement of Metamaterial Cavity






- Point source inside the cavity shows strong emission enhancement results.
- The acoustic wave field is strongly localized within the low impedance air gap.


## Emission Enhancement of Metamaterial Cavity






- 15 dB ( x 30 power, x 5.5 pressure ampitude) emission ennancement can be achieved.
- The incident wave ( $1000 \mathrm{~Hz}, \lambda=34 \mathrm{~cm}$ ) can be amplified in a cavity which has unit cell size of $1 \mathrm{~cm}(1 / 34)$ and length of $4 \mathrm{~cm}(\sim 1 / 9)$ subwavelength structure.


## Effective Control of Refractive Index and Impedance


$w=3 \mathrm{~mm}$

$w=5 \mathrm{~mm}$


1
$w=7 \mathrm{~mm}$





- Increasing the path length increases the refractive index since the effective speed of sound is reduced.

$$
\begin{array}{ll}
\mathrm{n}=\mathrm{c}_{\mathrm{o}} / \mathrm{c}_{1}, & \begin{array}{l}
\text { where } \\
\mathrm{n}=\text { refractive index, } \mathrm{c}_{\mathrm{o}}=\text { speed of sound in reference material } \\
\mathrm{c}=\text { speed of sound in medium }
\end{array}
\end{array}
$$

## Sonic Boost using Acoustic Metamaterial Cavity



- A microphone was place inside the metamaterial cavity to detect the amplified acoustic pressure from an outside source.


## Sonic Boost using Acoustic Metamaterial Cavity






- 15 dB ( x 30 power, x 5.5 pressure amplitude) emission enhancement can be achieved.
- The incident wave ( $1000 \mathrm{~Hz}, \lambda=34 \mathrm{~cm}$ ) can be amplified in a cavity which has unit cell size of $1 \mathrm{~cm}(1 / 34)$ and length of $3 \mathrm{~cm}(\sim 1 / 10)$ subwavelength structure.


## Independent Control of Refractive index and Impedance



- Strong pressure amplification due to increased impedance.
- High index of refraction reduces the resonance frequency.


## Effective Medium Theory and Reduced Particle Velocity





- Effective medium theory exactly replicates the sound pressure amplification results.
- Pressure is increased due to reduced particle velocity ( $P=I / c_{p}$ ).


## Underwater SPL Amplification

Further Enhancement using Quarter Wave
Resonator



SPL Amplification in an Underwater
Environment





